



# Mutational Signatures

February 20, 2020

CS 598 MEB

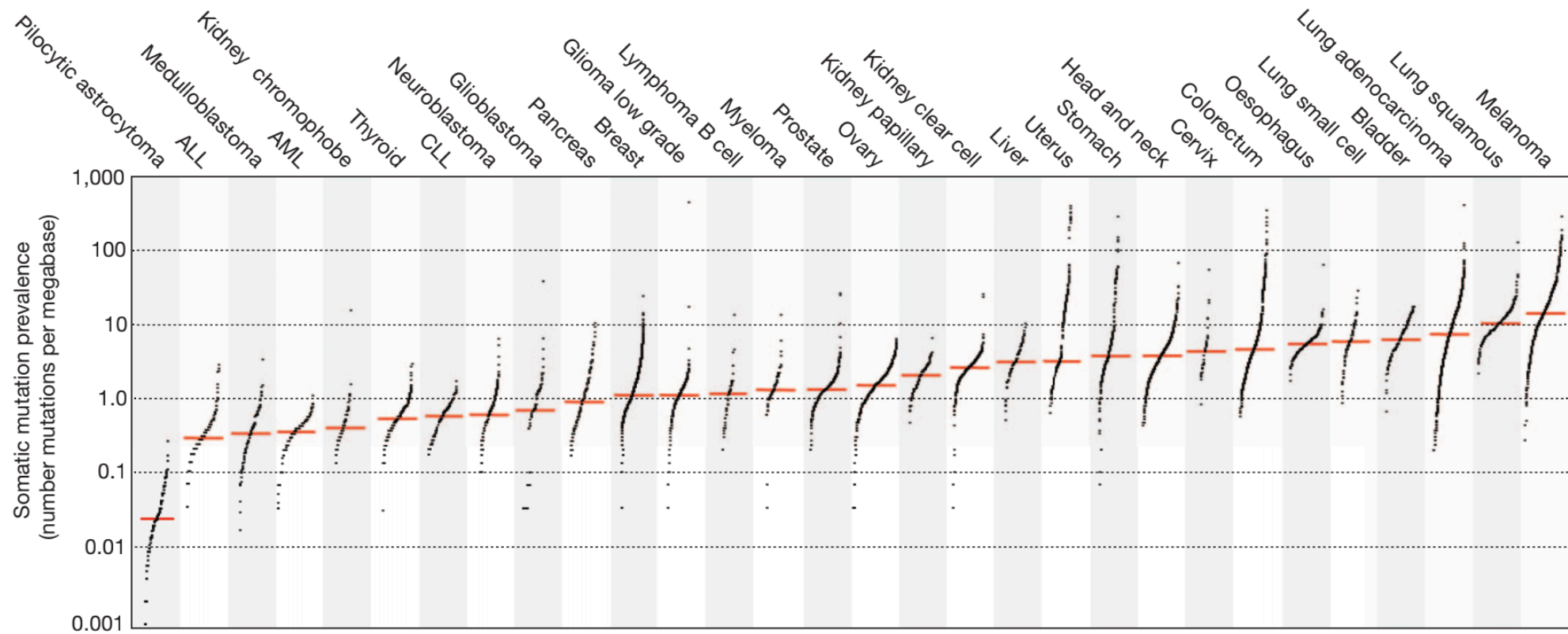
# Today's Outline

1. **What** are mutational signatures?
2. **How** are mutational signatures estimated?
3. **Why** are mutational signatures useful?

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# Prevalence of mutations in cancer

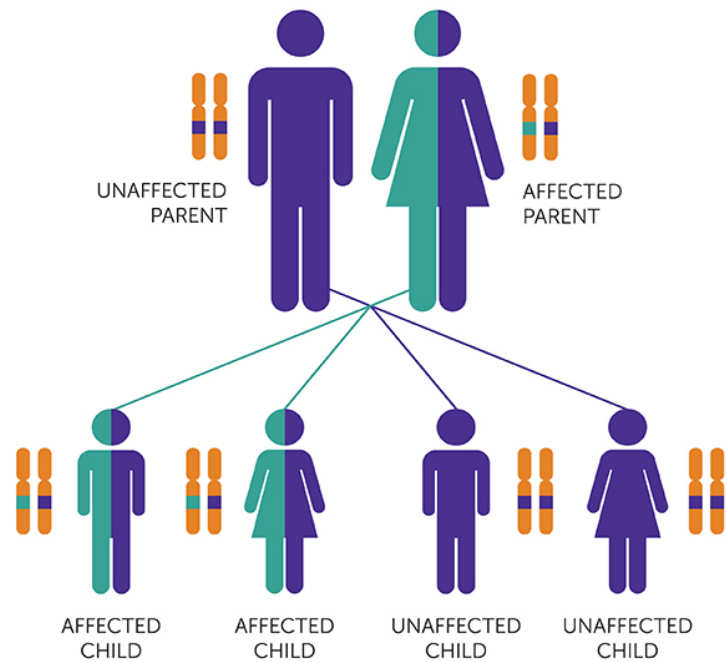


On average, 1,000-10,000 mutations/genome and 10-100 mutations/exome

# Where do mutations come from?

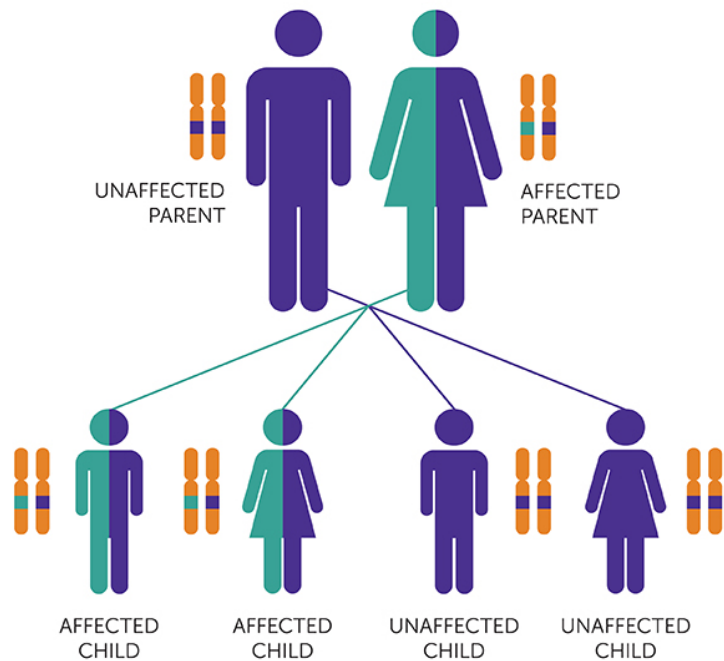
Germline

Somatic



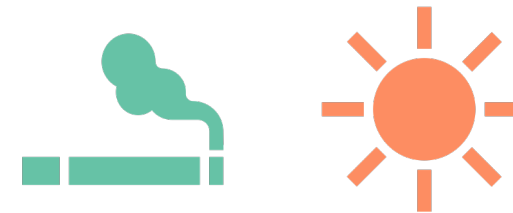
# Where do mutations come from?

## Germline



## Somatic

### *Environmental Interference*



### *Replication Errors*



# Somatic mutations accumulate over time

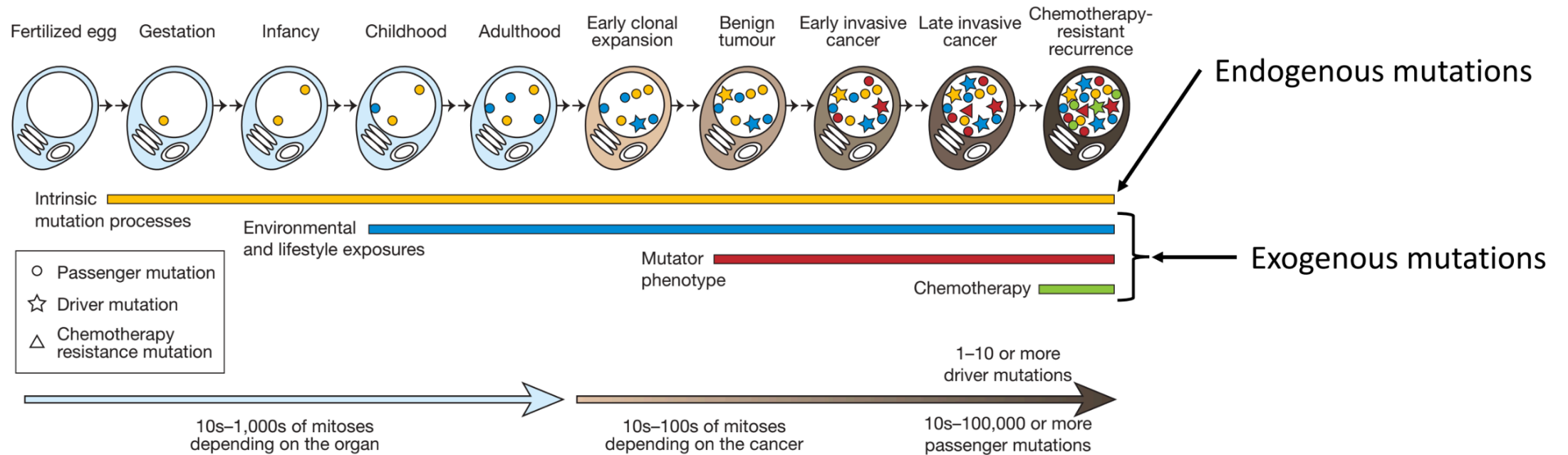
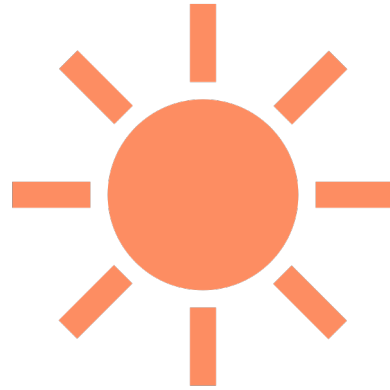


Figure 1: Stratton et al. (Nature 2009)

# Somatic mutations accumulate over time

GERMLINE: cagaccagatagggcatgagatacatccgcgagtgattggattacatctggggagtgattgatctaaactcttctcaagg

CANCER: aagacctagttagggcatgagaacatgcccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg





# Problem! No labels

GERMLINE: cagaccagatagggcatgagatacatccgcgagtgattggattacatctggggagtgattgatctaaactcttctcaagg

CANCER: aagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtgggtgattcatctaaagtcttcgcatgg

# Mutational Signatures

GOAL 1: Identify distinct mutational patterns associated with mutational processes (i.e., estimate *signatures*).

GOAL 2: Identify exposure to each pattern for each patient (i.e., estimate *exposures*).

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# Idea! Look across patients

PATIENT 1: aagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

PATIENT 2: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

PATIENT 3: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

•  
•  
•

PATIENT n: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

# Idea! Look across patients

PATIENT 1: aagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

PATIENT 2: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

PATIENT 3: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

•  
•  
•

PATIENT n: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

# What patterns should we look at?

PATIENT 1: aagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

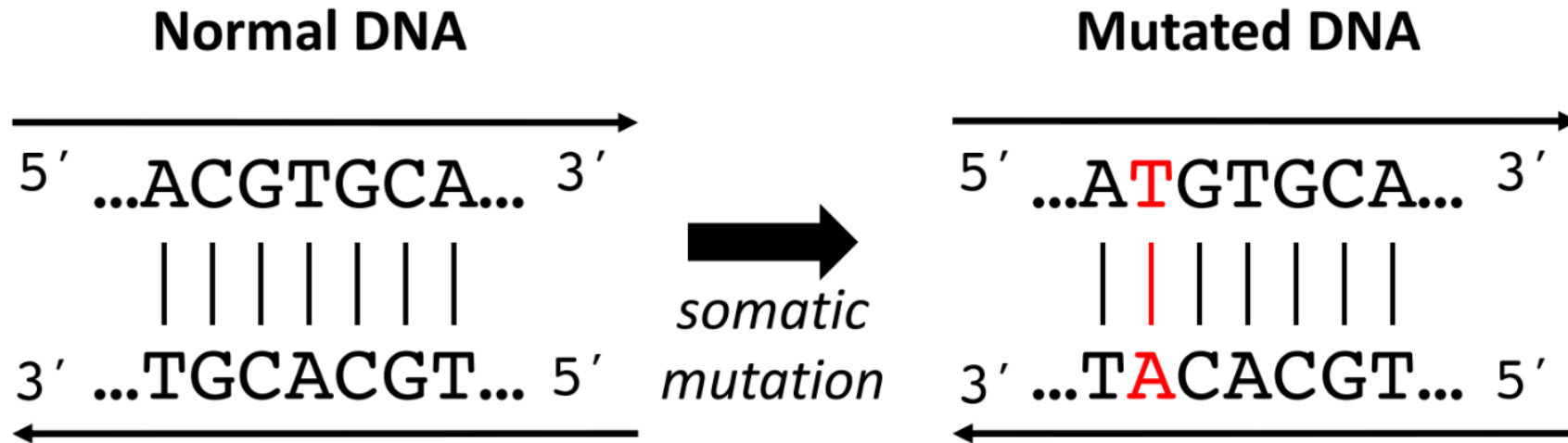
PATIENT 2: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

PATIENT 3: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

•  
•  
•

PATIENT n: agaagacctagttagggcatgagaacatgcgccagtgatcggaattcatgtgggtggtgattcatctaaagtcttcgcatgg

# Mutational Category: Single base substitutions



Did a C>T mutation occur? Or a G>A?

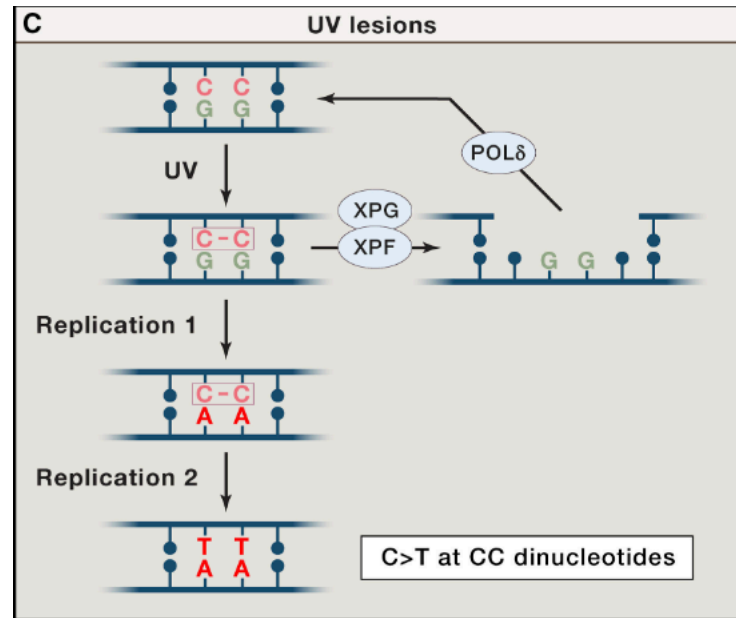
# Mutational Category: Single base substitutions

	A	T	C	G
T	T > A		T > C	T > G
C	C > A	C > T		C > G

Six substitutions patterns (pyrimidine first)



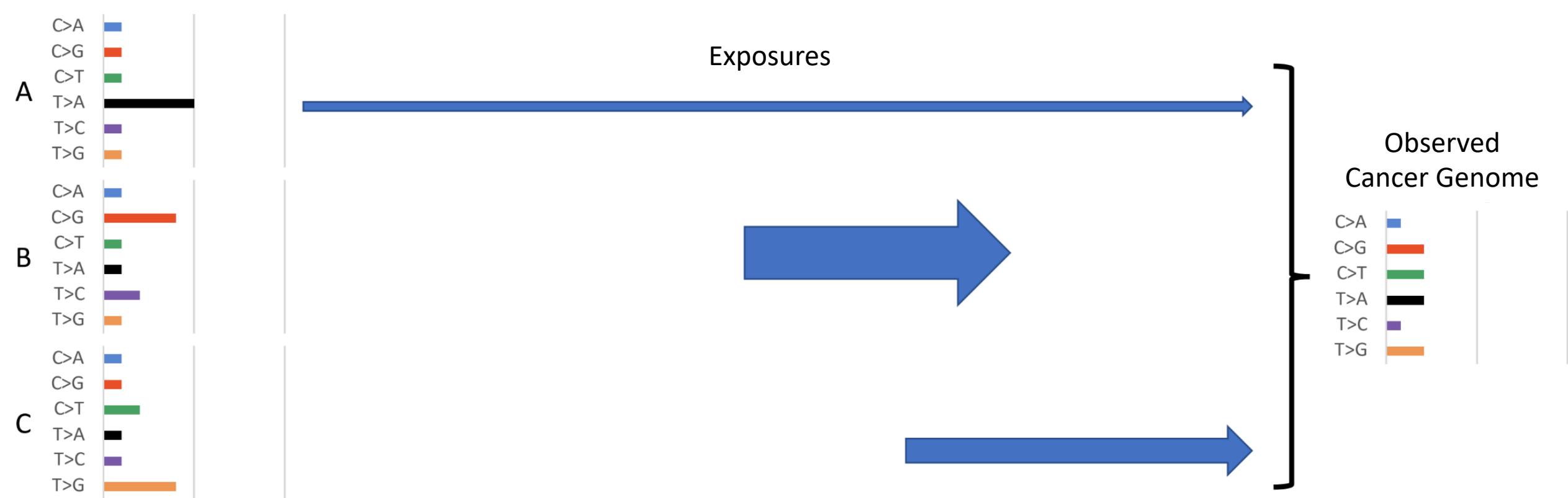
# Mutational Category: Single base substitutions



Environmental exposures and repair errors can lead to consistent substitution patterns.

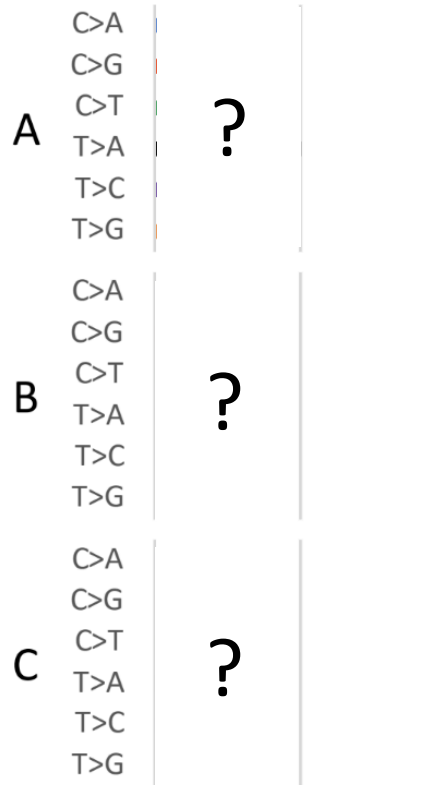
# Integrating mutational categories into problem

## Mutational Processes



# Integrating mutational categories into problem

Mutational Processes



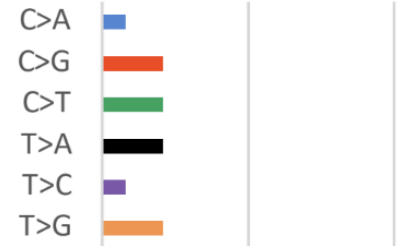
Exposures

?

?

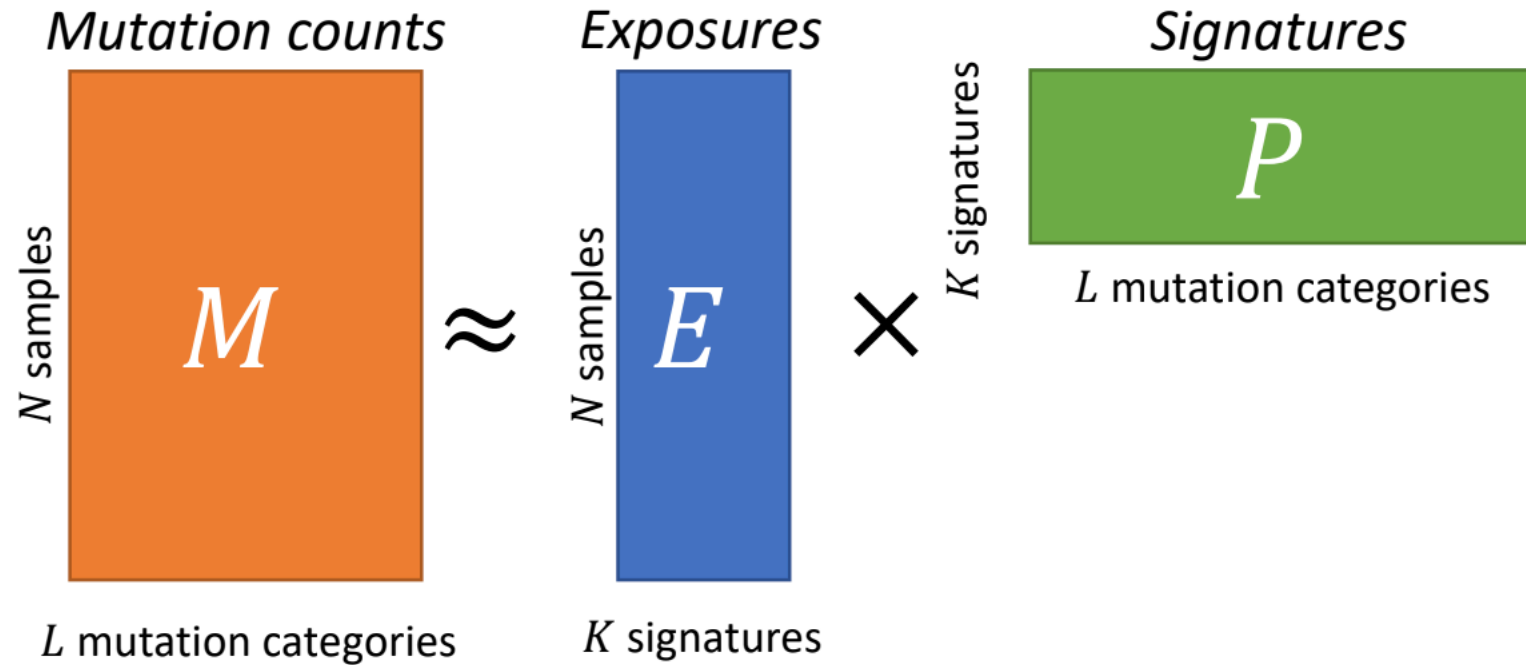
?

Observed  
Cancer Genome



Adapted from Ludmil Alexandrov

# Alexandrov Problem Statement



Objective function:







$$\min_{E, P} \|M - EP\|_2^2 \text{ such that } E, P \geq 0.$$





# Alexandrov Algorithmic Technique

## Non-negative Matrix Factorization (NMF)

- Unique solution not guaranteed
- Popular search heuristics use alternating optimization
- Used in many applications

	M1	M2	M3	M4	M5
 Comedy	3	1	1	3	1
 Action	1	2	4	1	3

	 Comedy	 Action
 A	✓	✗
 B	✗	✓
 C	✓	✗
 D	✓	✓

	M1	M2	M3	M4	M5
	3	1	1	3	1
	1	2	4	1	3
	3	1	1	3	1
	4	3	5	4	4

# Alexandrov Model Selection

The number of mutational processes is not known.

Algorithm is run over a range of values.

Pick number of processes based on:

- Low reconstruction error for number of processes
- Process reproducibility with random initializations

# Alexandrov Mutational Category: SBS with flanking

A      C > T      G

$$4 \times 6 \times 4 = 96$$

# Alexandrov Data (v2 - March 2015)

10,952 exomes and 1,048 whole-genomes

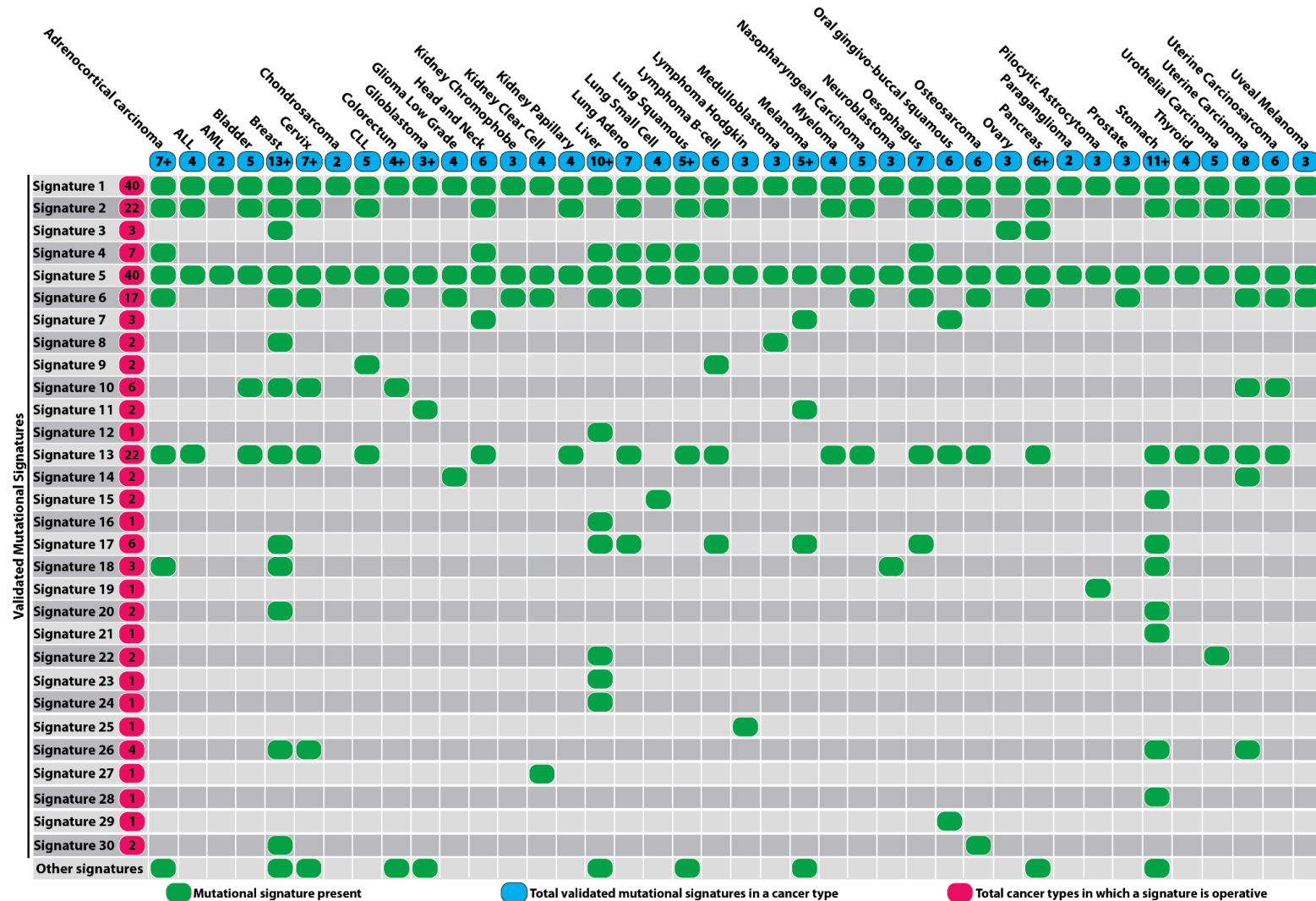
40 distinct types of human cancer

Estimated per cancer type and per class (WGS, WXS)

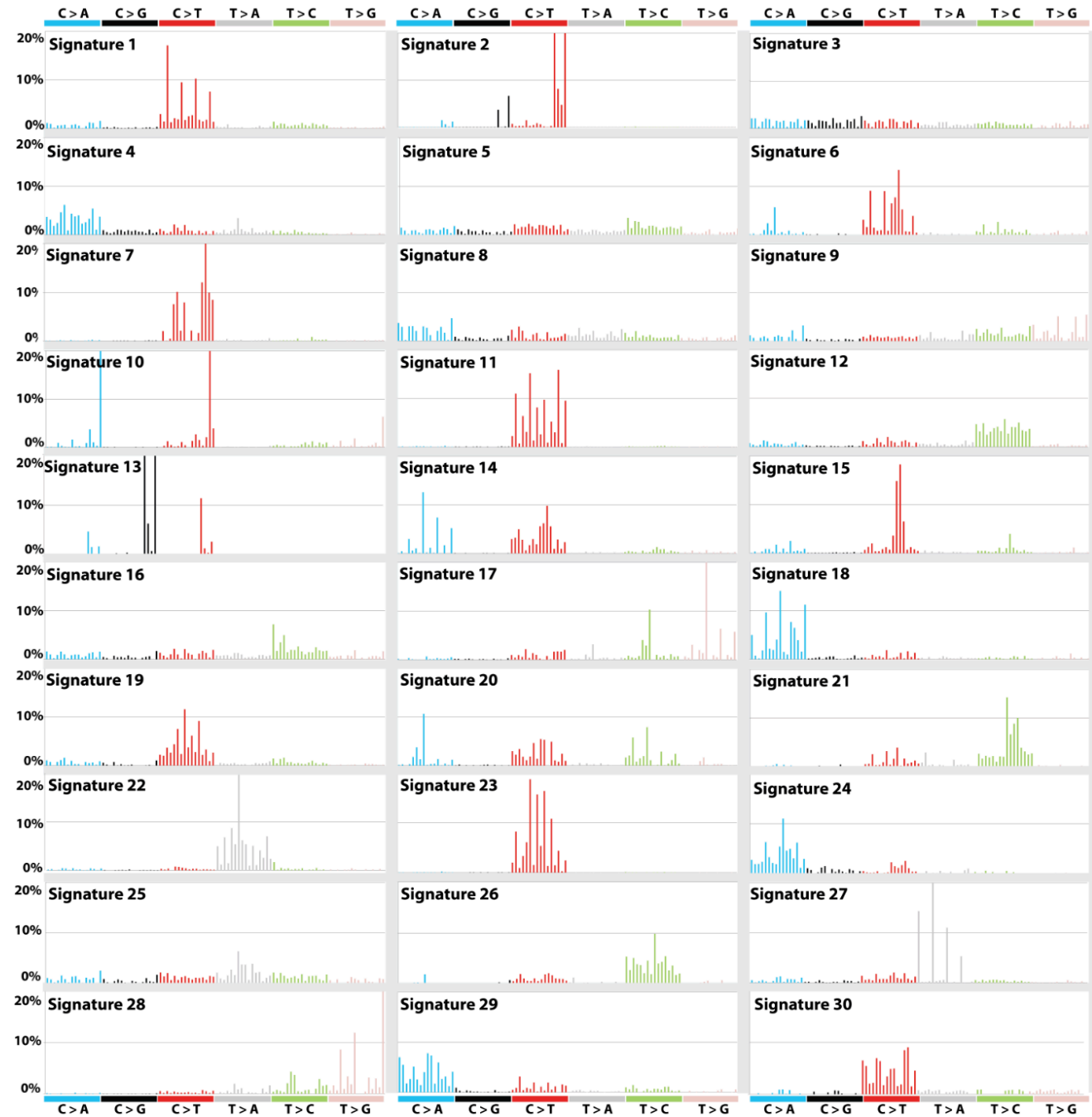
Maintained at: <https://cancer.sanger.ac.uk/cosmic/>



# Alexandrov Results (v2 - March 2015)



# Alexandrov Results (v2 - March 2015)



# Future Work

Improve the estimation of signatures

Look at different types of mutational categories

Study NMF solutions of comparable reconstruction error

Other ideas?

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# Application Directions

## Prevention

- Establish correlations between environmental factor and mutations

## Treatment

- Identify subtypes of patients based on signatures

Orthogonal signal for prioritizing solutions

# PhySigs: Phylogenetic Inference of Mutational Signature Dynamics

Sarah Christensen<sup>1</sup>, Mark D.M. Leiserson<sup>2</sup>, and Mohammed El-Kebir<sup>1</sup>

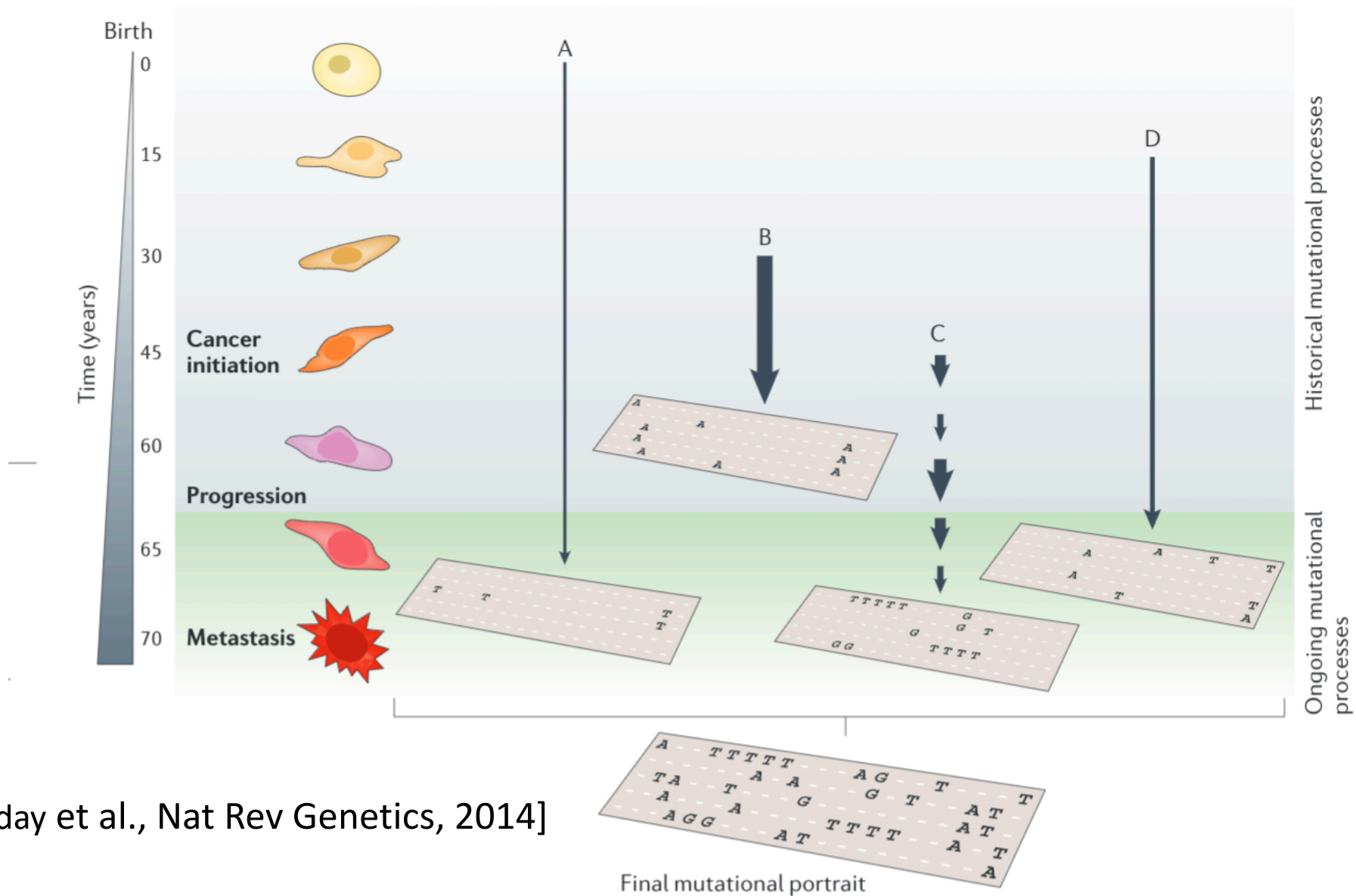
<sup>1</sup>Dept. of CS, University of Illinois at Urbana-Champaign

<sup>2</sup>Dept. of CS, University of Maryland College Park

PSB 2020



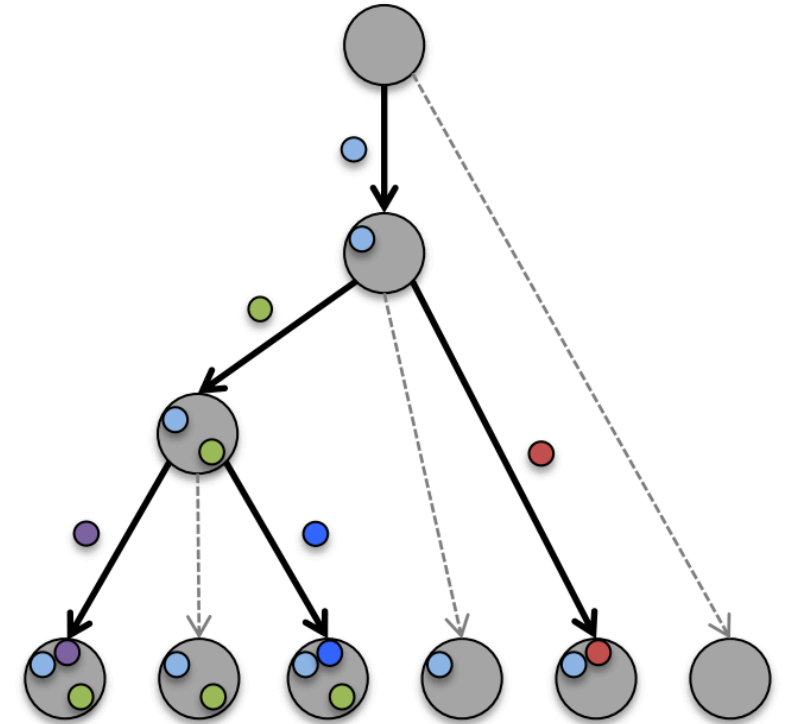
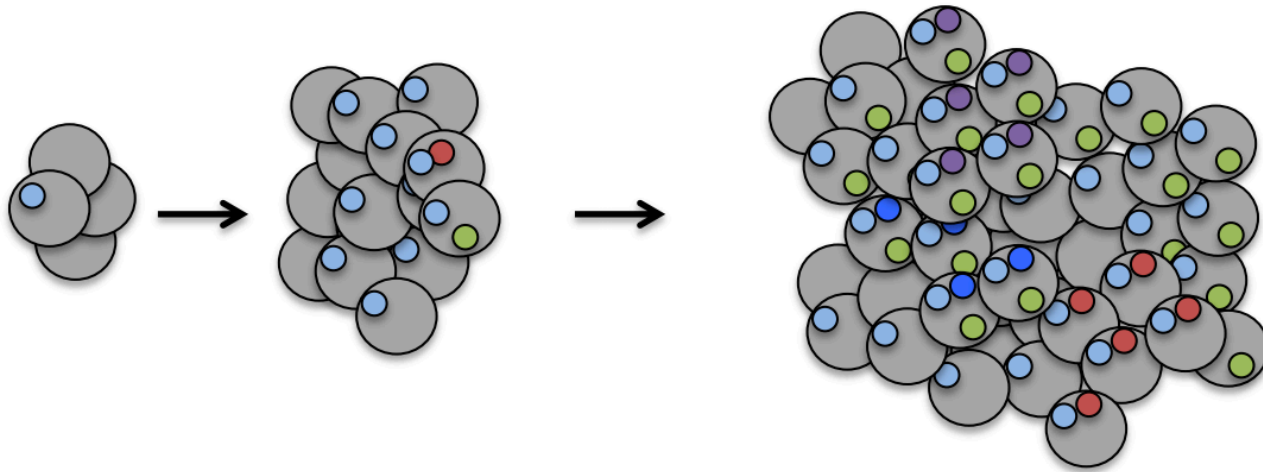
# Signature Exposures at the Tumor Level



[Helleday et al., Nat Rev Genetics, 2014]

# Intra-tumor Heterogeneity

## Clonal Evolution Theory of Cancer [Nowell, 1976]



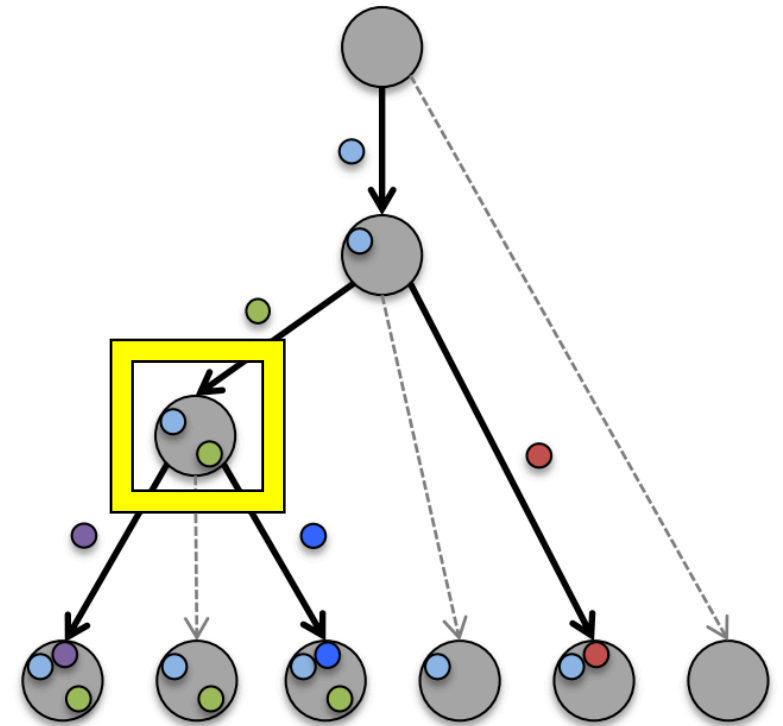
[Schwartz and Schäffer, Nat Rev Genetics, 2017]



# Heterogeneity in Signatures in Tumor Clones?

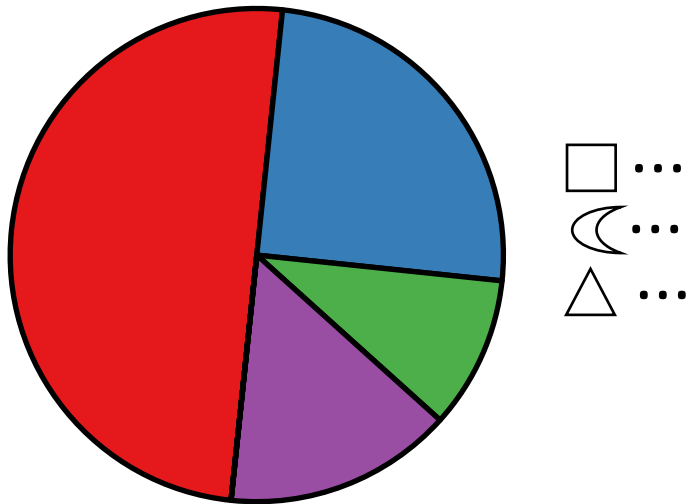
A clone can be distinguished from its parent by the set of newly introduced mutations.

Idea is to look at differences in exposures for these *newly introduced* mutations across the tree.

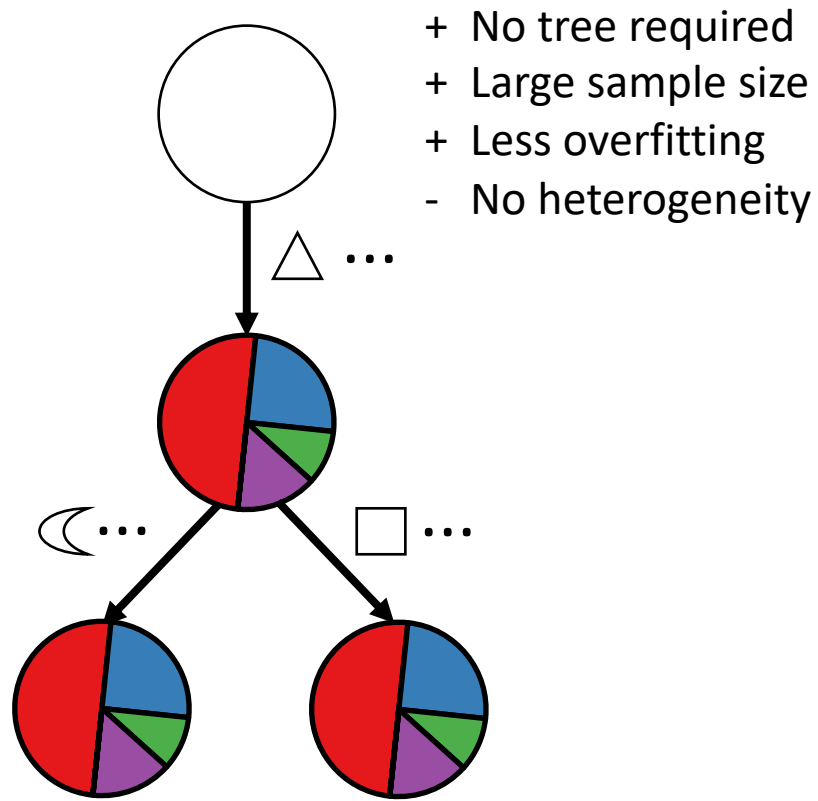


# Previous: Single Exposure Inference

■ sig. 1   ■ sig. 2   ...   ■ sig. 30



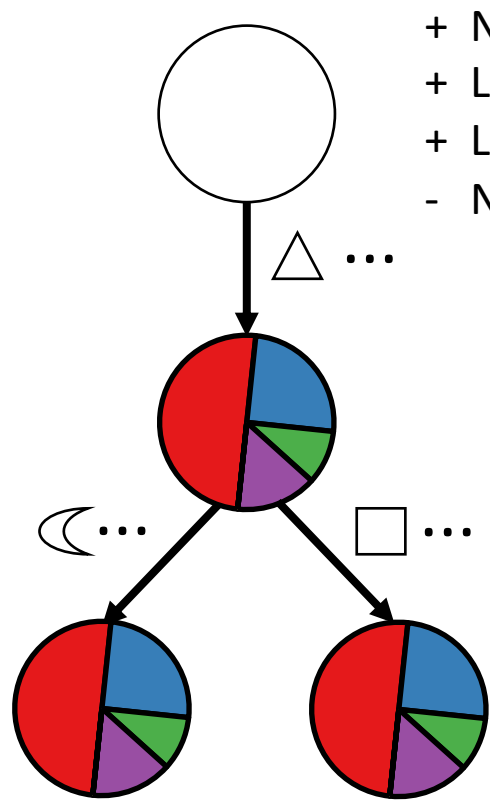
# Previous: Single Exposure Inference



- + No tree required
- + Large sample size
- + Less overfitting
- No heterogeneity

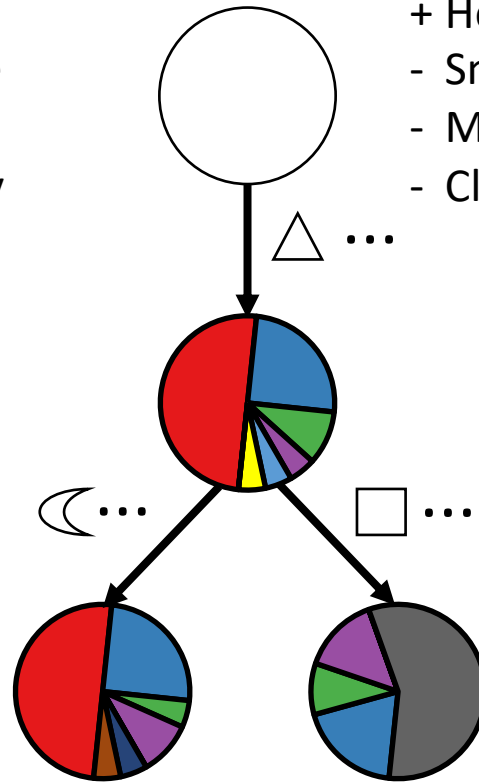
**Same** exposures for every clone

# Previous: Independent Exposure Inference



- + No tree required
- + Large sample size
- + Less overfitting
- No heterogeneity

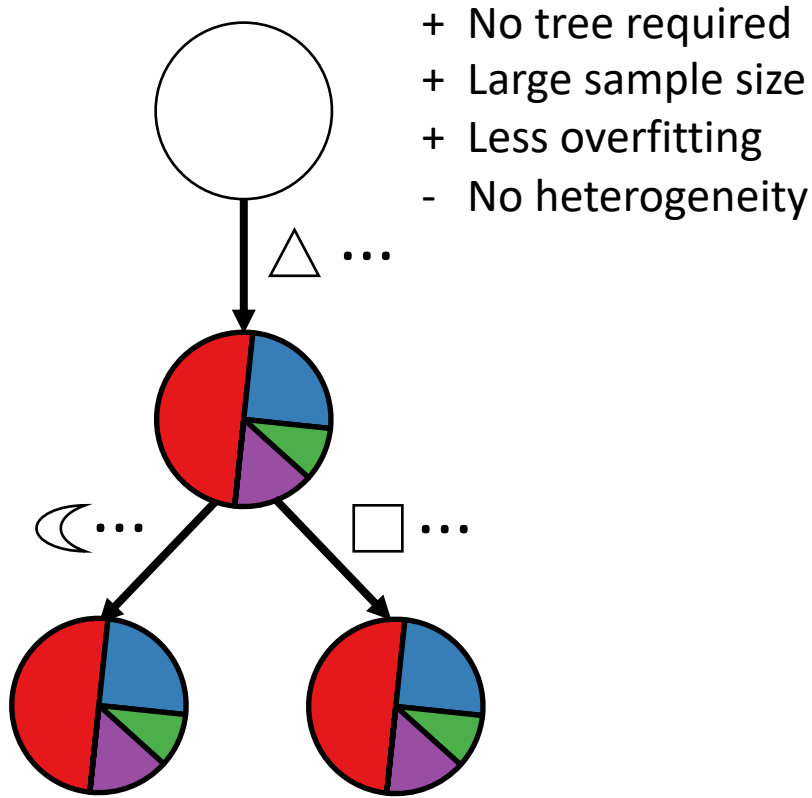
**Same** exposures for every clone



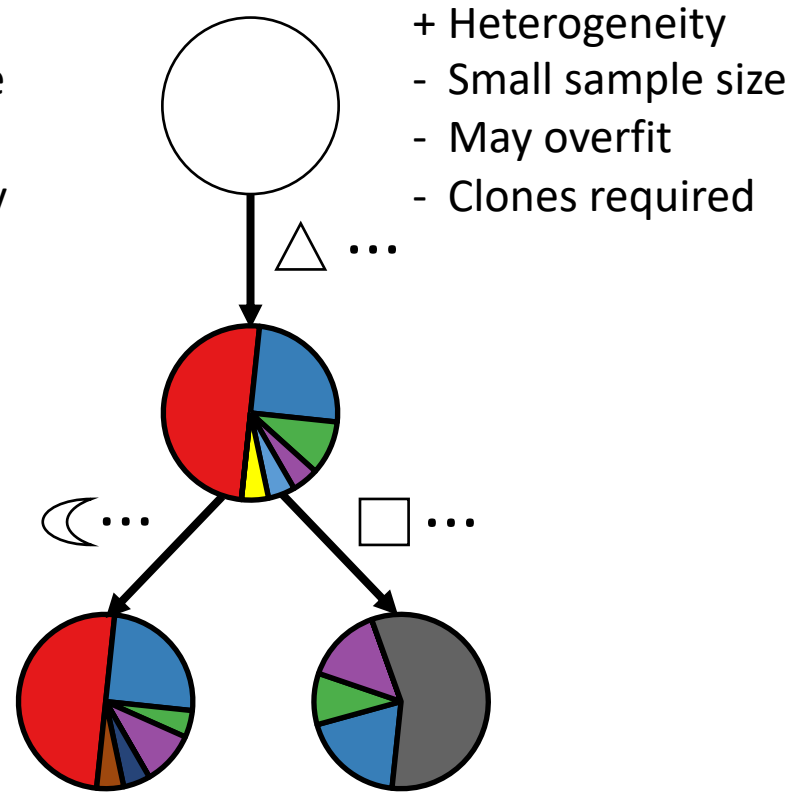
- + Heterogeneity
- Small sample size
- May overfit
- Clones required

**Different** exposures for every clone

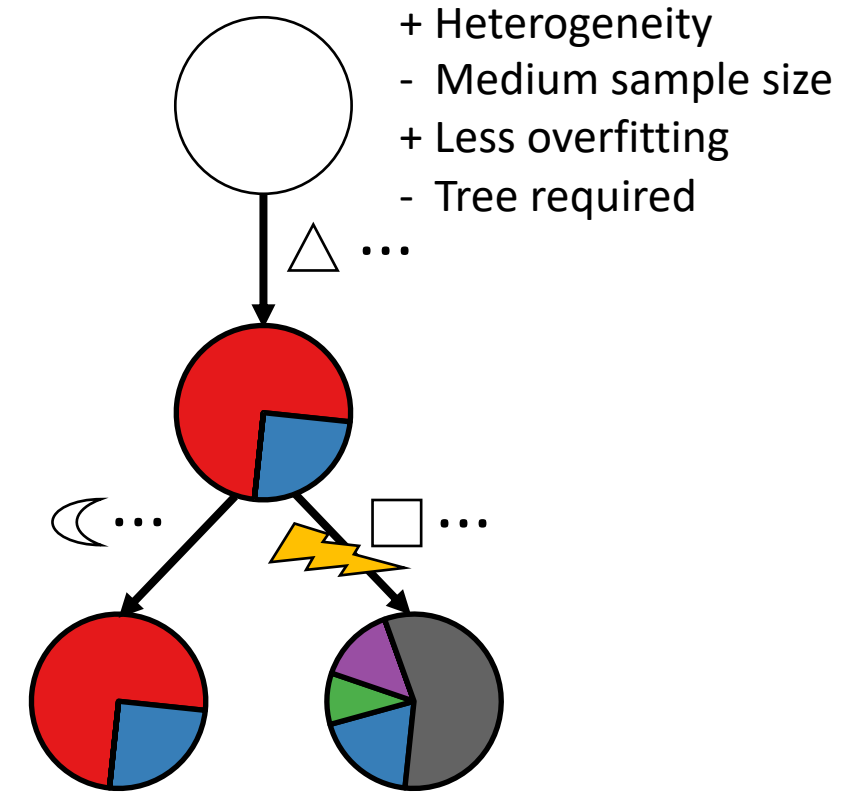
# This Work: Tree Constrained Exposure Inference



**Same** exposures for every clone



**Different** exposures for every clone



Clone exposures separated by **shifts**

# PhySigs

Problem Statement and Methodology

# Tree-constrained Exposure Problem

**Problem 3 (Tree-constrained Exposure (TE)).** Given feature matrix  $P$ , corresponding count matrix  $C$ , signature matrix  $S$ , phylogenetic tree  $T$  and integer  $k \geq 1$ , find relative exposure matrix  $D$  such that  $\|P - SDC\|_F$  is minimum and  $D$  is composed of  $k$  sets of identical columns, each corresponding to a connected subtree of  $T$ .

$P$ : Mutation Count Matrix

$$\begin{matrix} & \text{AC>AA} & \text{TC>GG} & & \\ & \begin{matrix} \triangle & \circ & \square \\ \triangle & & \square \end{matrix} & & \\ \begin{matrix} \text{AC>AA} \\ \text{TC>GG} \end{matrix} & \begin{pmatrix} 0 & 0 & 1 \\ 2 & 1 & 1 \end{pmatrix} & & & \end{matrix}$$

$$m \times n$$

# Tree-constrained Exposure Problem

**Problem 3 (Tree-constrained Exposure (TE)).** Given feature matrix  $P$ , corresponding count matrix  $C$ , signature matrix  $S$ , phylogenetic tree  $T$  and integer  $k \geq 1$ , find relative exposure matrix  $D$  such that  $\|P - SDC\|_F$  is minimum and  $D$  is composed of  $k$  sets of identical columns, each corresponding to a connected subtree of  $T$ .

$P$ : Mutation Count Matrix       $S$ : Signature Matrix

$$\begin{array}{c}
 \begin{array}{ccc}
 \textcircled{\triangle\triangle} & \textcircled{\curvearrowright} & \textcircled{\square\square} \\
 \text{AC>AA TC>GG} & & \\
 \begin{pmatrix} 0 & 0 & 1 \\ 2 & 1 & 1 \end{pmatrix} & \approx & \begin{array}{cc} \text{Sig. 1} & \text{Sig. 2} \\ \begin{pmatrix} 0 & .5 \\ 1 & .5 \end{pmatrix} \end{array} \\
 m \times n & & m \times r
 \end{array}
 \end{array}$$



# Tree-constrained Exposure Problem

**Problem 3 (Tree-constrained Exposure (TE)).** Given feature matrix  $P$ , corresponding count matrix  $C$ , signature matrix  $S$ , phylogenetic tree  $T$  and integer  $k \geq 1$ , find relative exposure matrix  $D$  such that  $\|P - SDC\|_F$  is minimum and  $D$  is composed of  $k$  sets of identical columns, each corresponding to a connected subtree of  $T$ .

$P$ : Mutation Count Matrix

$S$ : Signature Matrix

$D$ : Relative Exposure Matrix

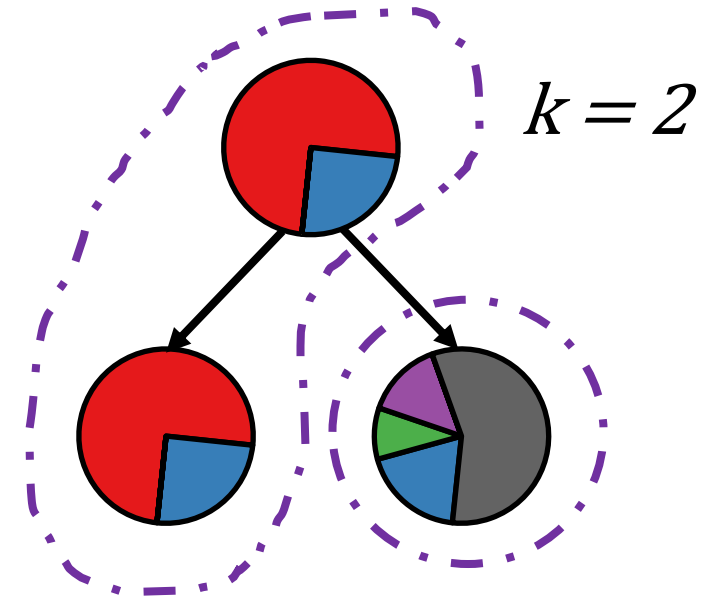
$C$ : Weight Matrix

$$\begin{array}{c}
 \begin{array}{ccc}
 \begin{array}{c} \triangle \triangle \\ \circlearrowleft \end{array} & \begin{array}{c} \circlearrowleft \end{array} & \begin{array}{c} \square \square \\ \circlearrowleft \end{array} \\
 \begin{array}{c} AC>AA \\ TC>GG \end{array} \begin{pmatrix} 0 & 0 & 1 \\ 2 & 1 & 1 \end{pmatrix} \approx \begin{array}{cc} \text{Sig. 1} & \text{Sig. 2} \\ \begin{array}{c} AC>AA \\ TC>GG \end{array} \begin{pmatrix} 0 & .5 \\ 1 & .5 \end{pmatrix} & \begin{array}{cc} \begin{array}{c} \triangle \triangle \\ \circlearrowleft \end{array} & \begin{array}{c} \circlearrowleft \end{array} \\ \begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix} & \begin{array}{c} \begin{array}{c} \square \square \\ \circlearrowleft \end{array} \\ 0 & 1 \end{array} & \begin{array}{ccc} \begin{array}{c} \triangle \triangle \\ \circlearrowleft \end{array} & \begin{array}{c} \circlearrowleft \end{array} & \begin{array}{c} \square \square \\ \circlearrowleft \end{array} \\ \begin{pmatrix} 2 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 2 \end{pmatrix} & \begin{array}{c} \triangle \triangle \\ \circlearrowleft \end{array} & \begin{array}{c} \circlearrowleft \end{array} & \begin{array}{c} \square \square \\ \circlearrowleft \end{array} \\
 \begin{array}{c} m \times n \end{array} & \begin{array}{c} m \times r \end{array} & \begin{array}{c} r \times n \end{array} & \begin{array}{c} n \times n \end{array}
 \end{array}
 \end{array}
 \end{array}$$

$E$ : Exposure Matrix

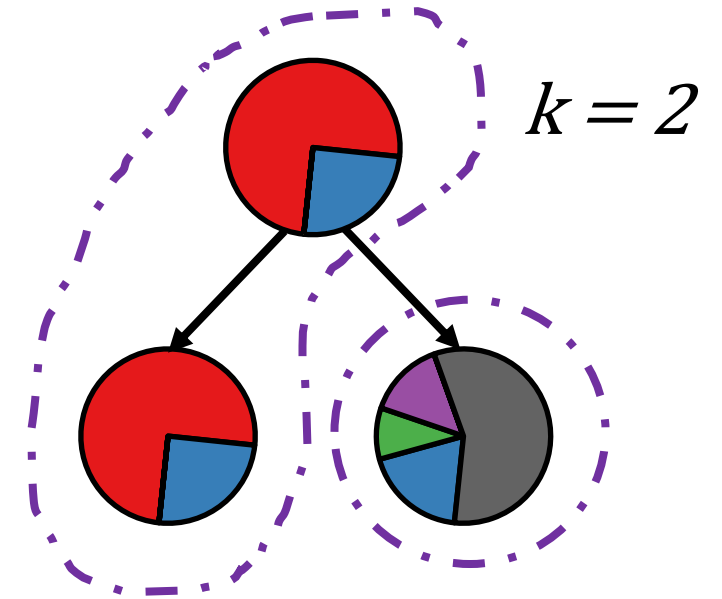
# PhySigs Algorithm

Step 1: Solve TE Problem for each possible number  $k$  of clusters

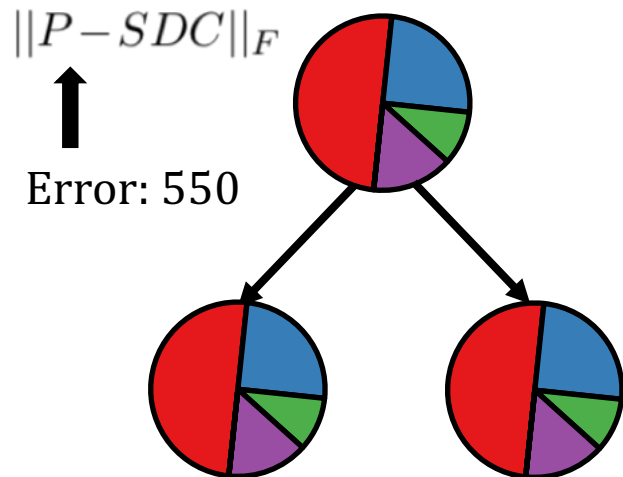


# PhySigs Algorithm

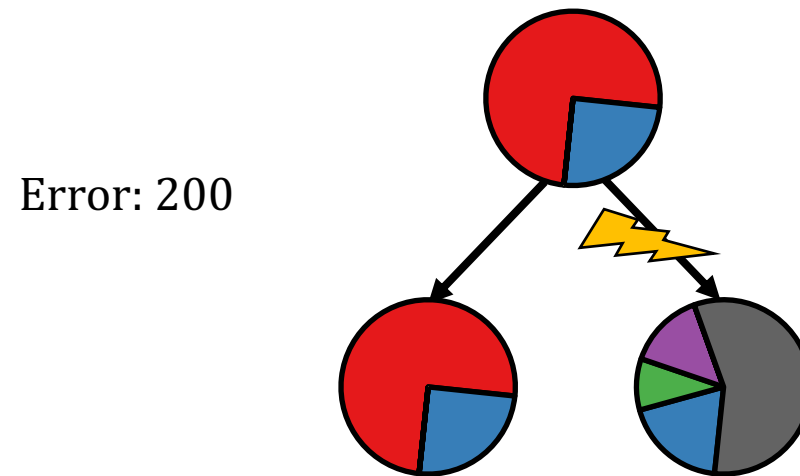
Step 1: Solve TE Problem for each possible number  $k$  of clusters



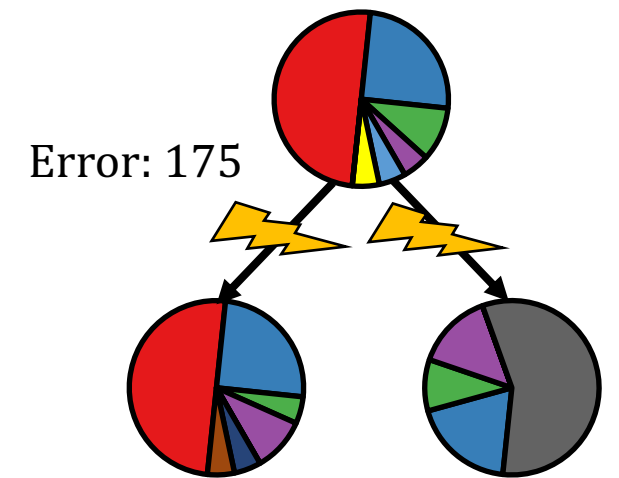
*No Shift ( $k=1$ )*



*One Shift ( $k=2$ )*



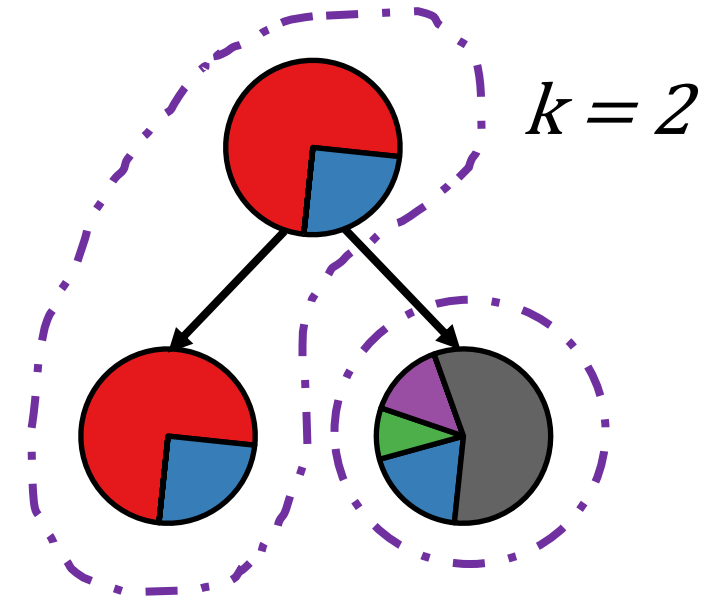
*Two Shifts ( $k=3$ )*



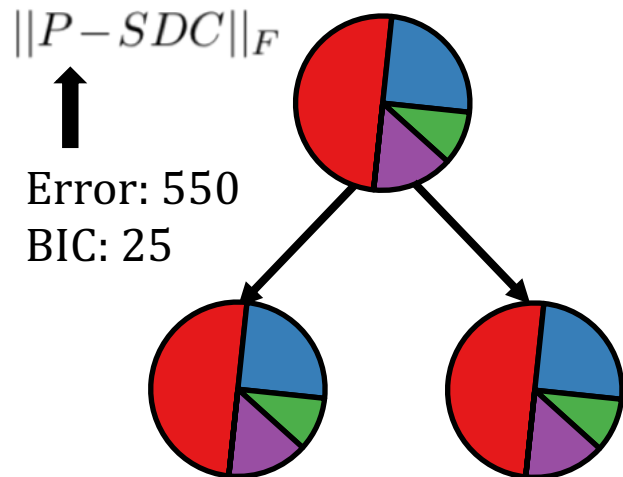
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Step 1: Solve TE Problem for each possible number  $k$  of clusters

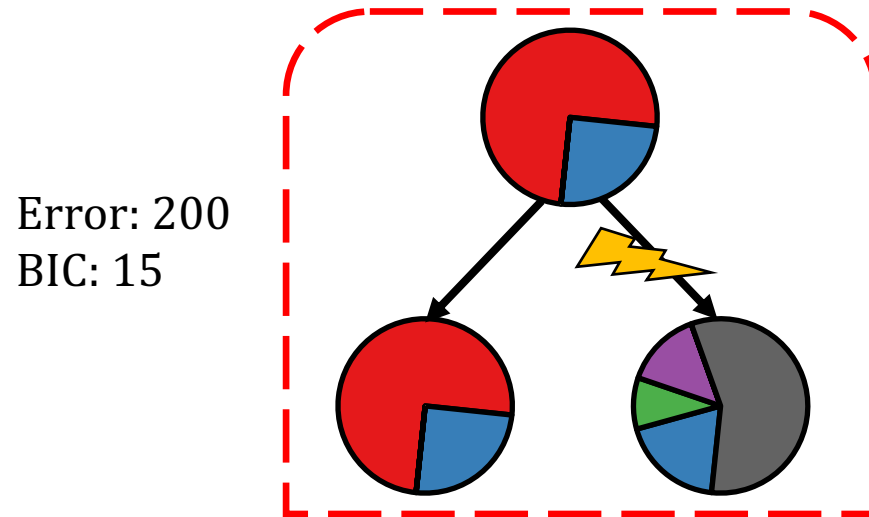
Step 2: Choose best number  $k$  of clusters using Bayesian Information Criterion (BIC)



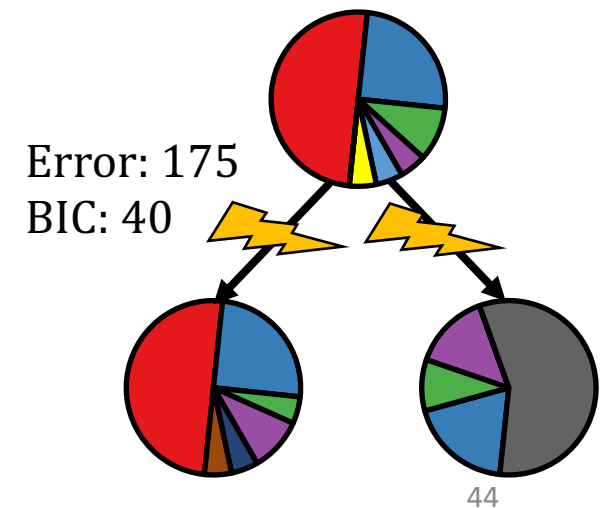
*No Shift (k=1)*



*One Shift (k=2)*



*Two Shifts (k=3)*

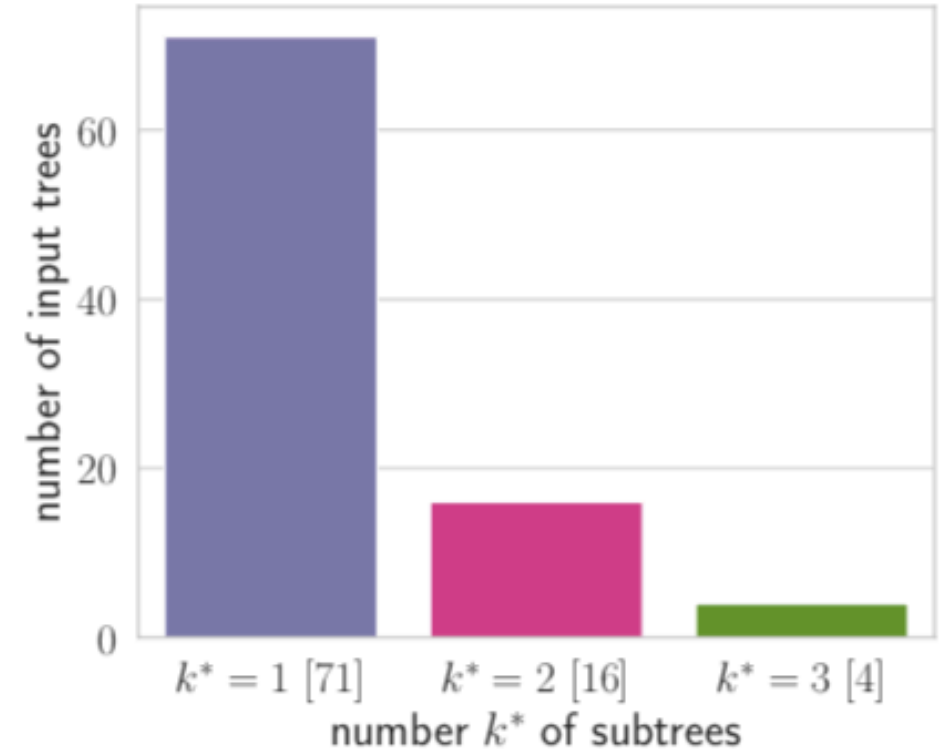


# Results

On Simulated and Biological Data

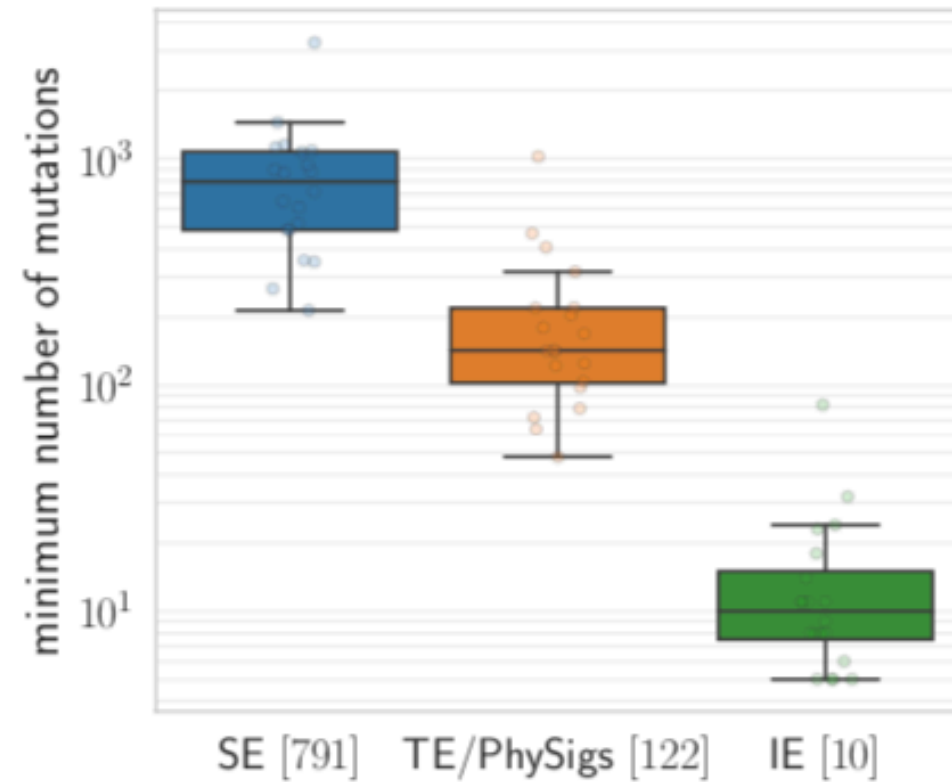
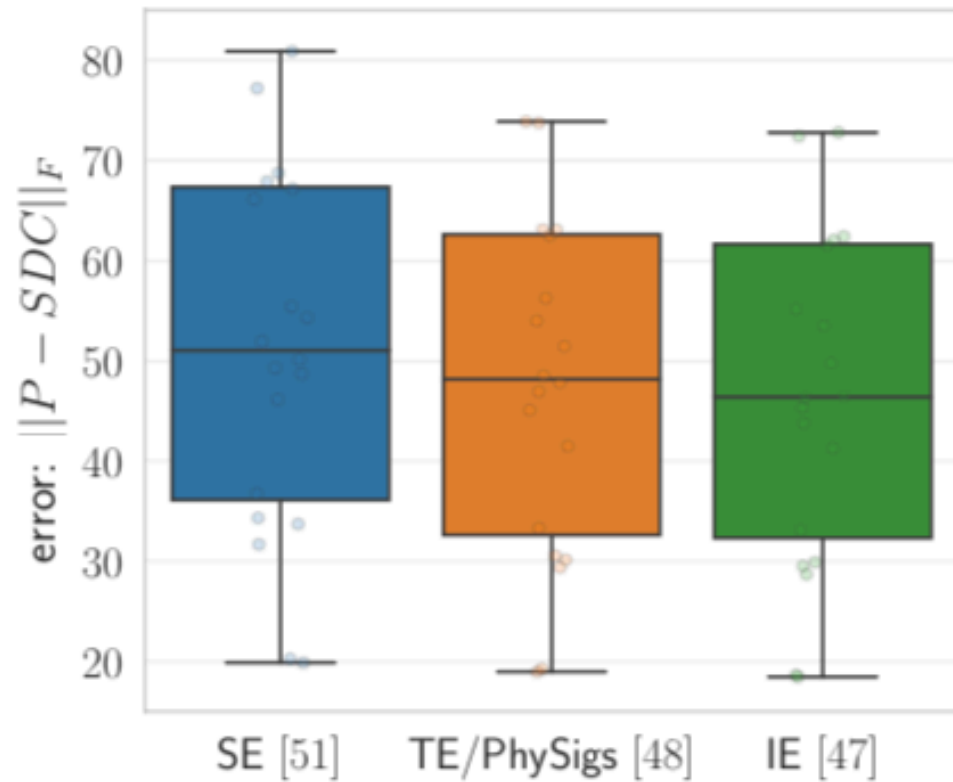
# PhySigs on Lung Cancer Cohort

- 91 patient tumors
- Number of clones per patient ranges from 2 to 15 (median of 5).
- Number of equally likely trees per patient ranges from 1 to 17 (median of 1).



Data from [Jamal-Hanjani et al., 2017]

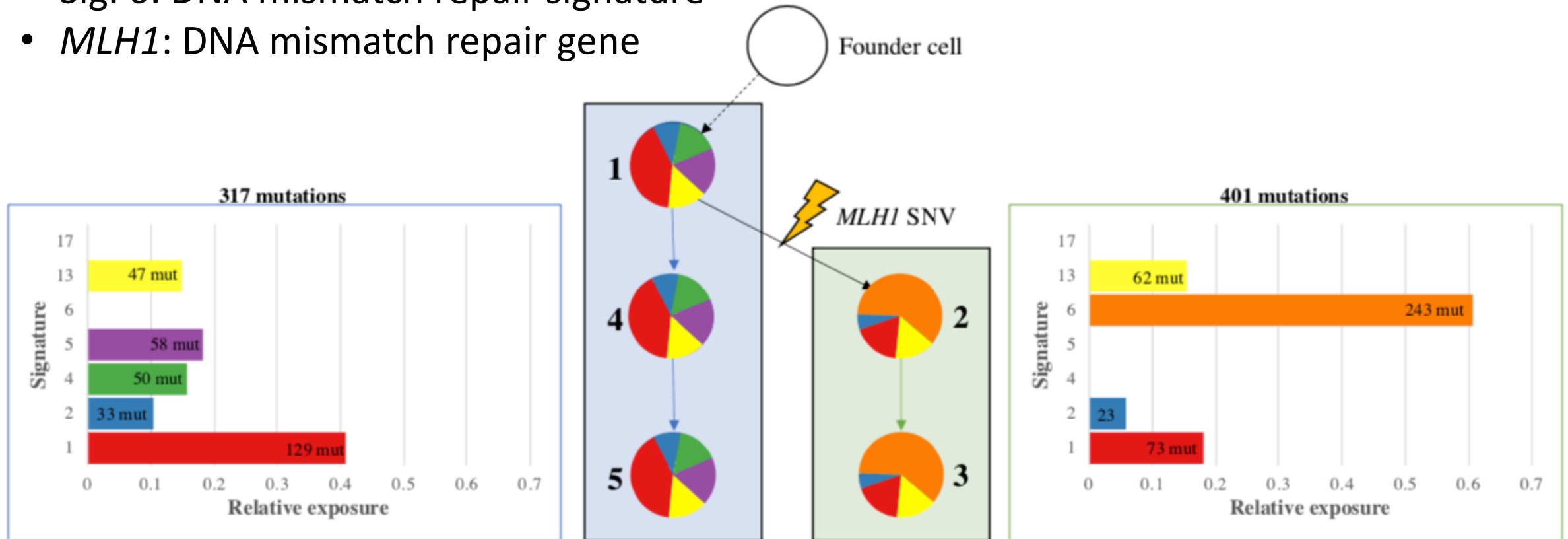
# PhySigs Explains Data without Overfitting



Data from [Jamal-Hanjani et al., 2017]

# PhySigs Finds Explainable Shift for Patient CRUK0064

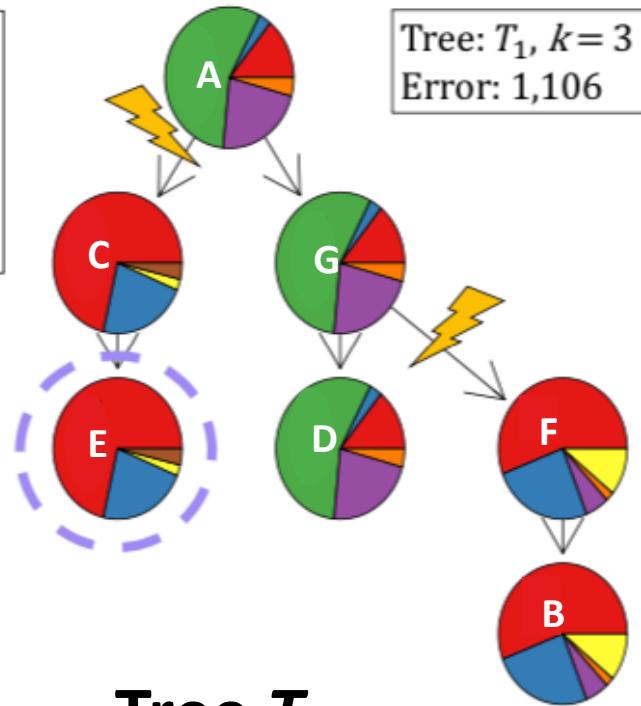
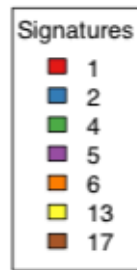
- Sig. 6: DNA mismatch repair signature
- *MLH1*: DNA mismatch repair gene



Data from [Jamal-Hanjani et al., 2017]

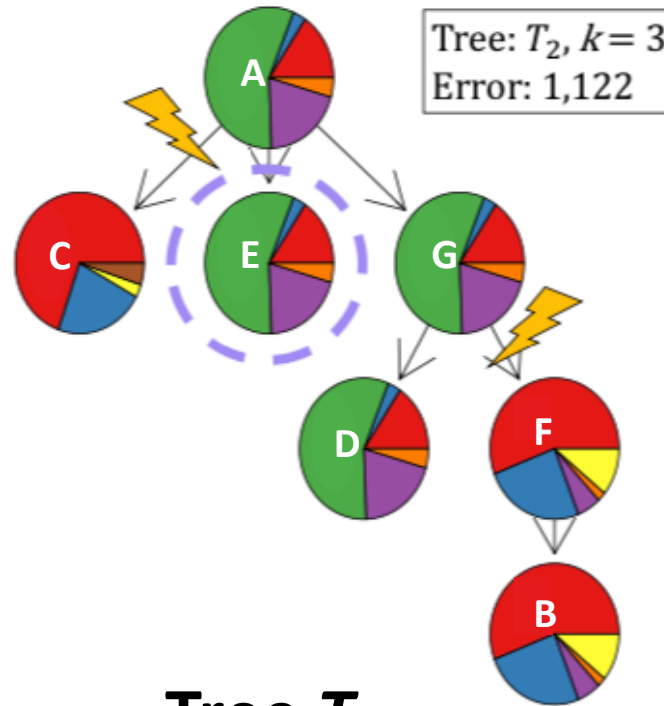


# PhySigs Constrains Solutions for Patient CRUK0025



**Tree  $T_1$**

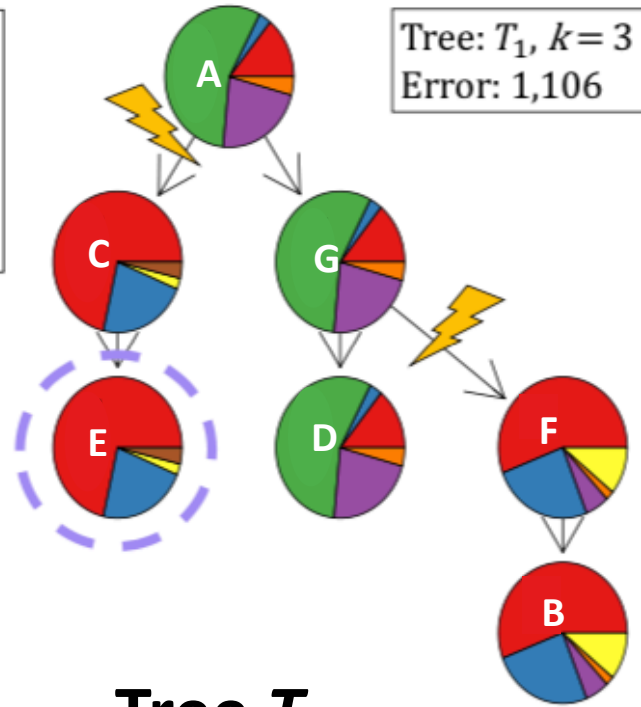
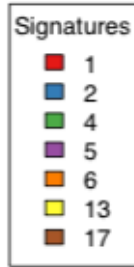
- 2 Shifts
- Small Error



**Tree  $T_2$**

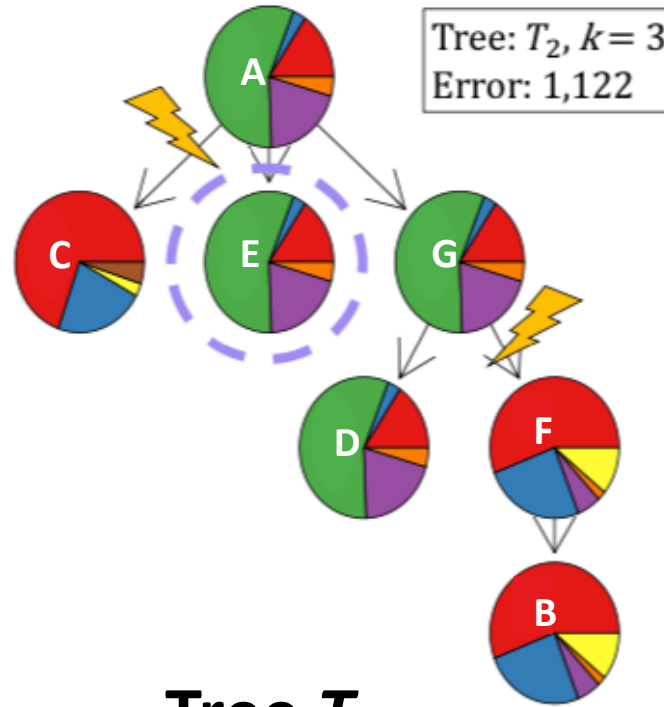
- 2 Shifts
- Big Error

# PhySigs Constrains Solutions for Patient CRUK0025



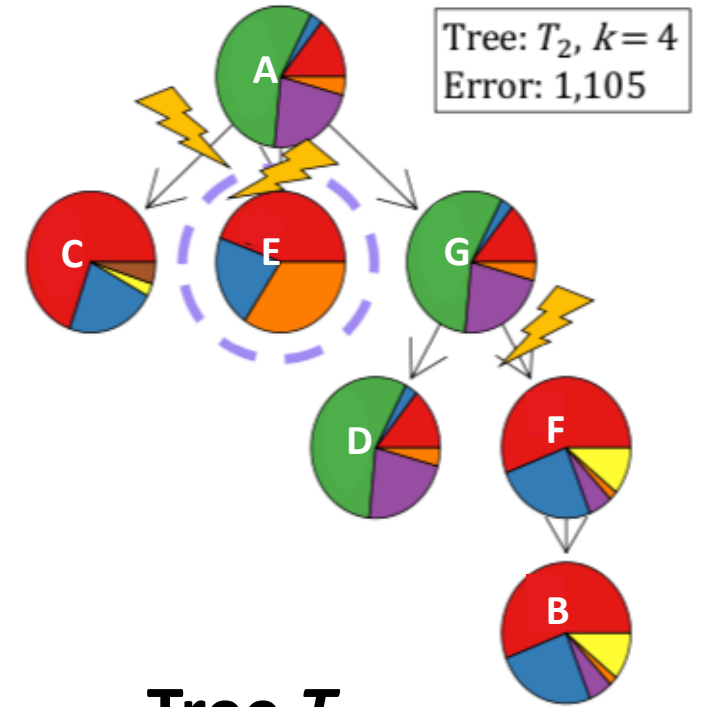
**Tree  $T_1$**

- 2 Shifts
- Small Error



**Tree  $T_2$**

- 2 Shifts
- Big Error



**Tree  $T_2$**

- 3 Shifts
- Small Error

# Conclusions and Discussion

Key concept: mutational signature exposure may not be constant across clones due to intra-tumor heterogeneity

PhySigs identifies shifts along edges of a tumor's evolutionary tree

- May want to consider additional patterns for shifts

PhySigs works by reducing to single exposure problem and then can be solved with existing algorithms

- Hardness of tree constrained exposure for a fixed  $k$  remains open

Availability: <https://github.com/elkebir-group/PhySigs>

# Acknowledgements

## **El-Kebir lab:**

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- Yerong Li
- Yuanyuan Qi



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