# CS 466 Introduction to Bioinformatics Lecture 4

Mohammed El-Kebir September 5, 2021



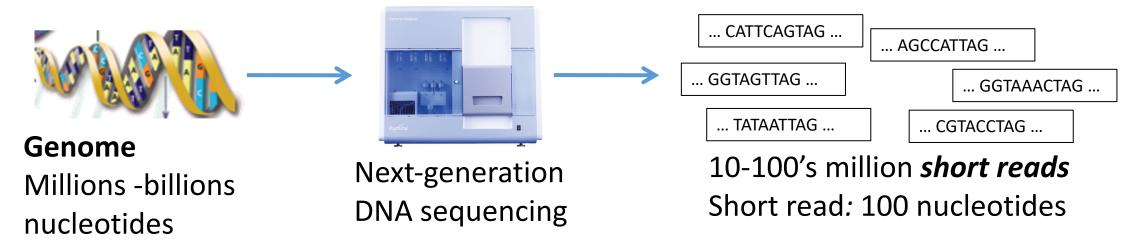
## Outline

- 1. Fitting alignment
- 2. Local alignment
- 3. Gapped alignment
- 4. BLOSUM scoring matrix

#### Reading:

- Jones and Pevzner. Chapters 6.6-6.9
- Lecture notes

## NGS Characterized by Short Reads



#### Allow for inexact matches due to:

- Sequencing errors
- Polymorphisms/mutations in reference genome

Human reference genome is 3,300,000,000 nucleotides, while a short read is 100 nucleotides. Global sequence alignment will not work!

**Question**: How to account for discrepancy between lengths of reference and short read?

## Fitting Alignment

For short read alignment, we want to align complete short read  $\mathbf{v} \in \Sigma^m$  to substring of reference genome  $\mathbf{w} \in \Sigma^n$ . Note that  $m \ll n$ .

$$\mathbf{w} \in \Sigma^n$$

$$\mathbf{v} \in \Sigma^m$$

## Fitting Alignment – Naive Approach

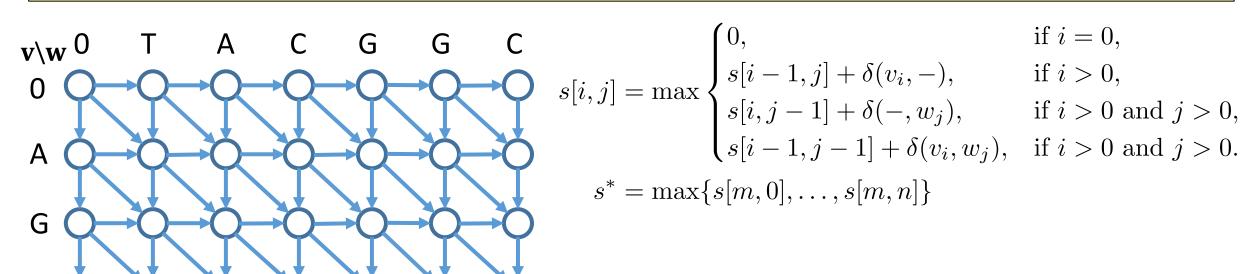
$$\mathbf{w} \in \Sigma^n$$

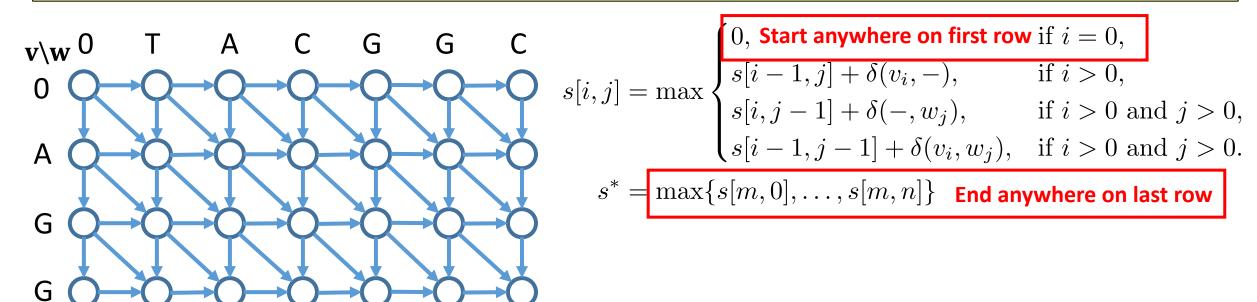
- Consider all contiguous non-empty substrings of **w**, defined by  $1 \le i \le j \le n$
- How many?

## Fitting Alignment – Naive Approach

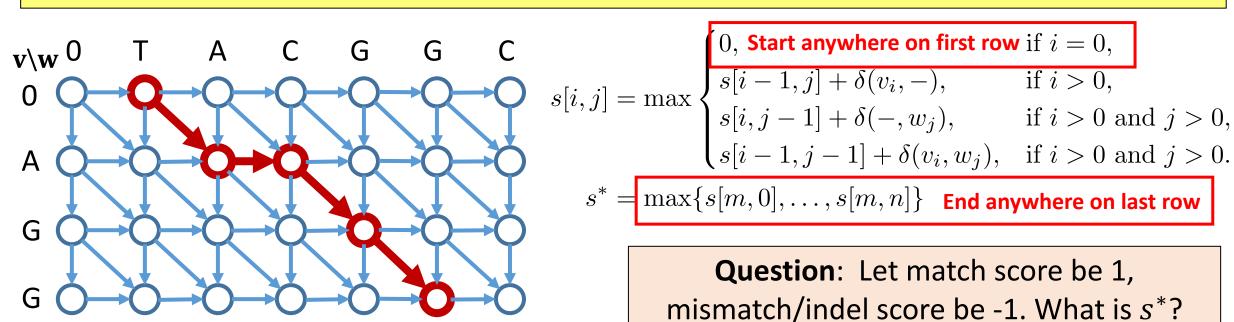
$$\mathbf{w} \in \Sigma^n$$

- Consider all contiguous non-empty substrings of  $\mathbf{w}$ , defined by  $1 \le i \le j \le n$
- How many? Answer:  $n + \binom{n}{2}$
- What are their total lengths?
- What is the running time?





Fitting Alignment problem: Given strings  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  and scoring function  $\delta$ , find an alignment of  $\mathbf{v}$  and a substring of  $\mathbf{w}$  with maximum global alignment score  $s^*$  among *all* global alignments of  $\mathbf{v}$  and *all* substrings of  $\mathbf{w}$ 



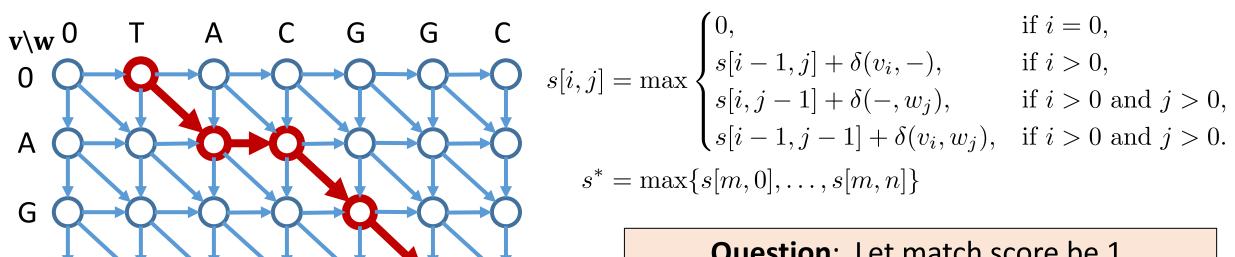
 V
 A
 G
 G

 W
 T
 A
 C
 G
 G
 C

**Question**: Same scores. What is optimal global alignment and score?

#### • Online:

https://valiec.github.io/AlignmentVisualizer/index.html



**Question**: Let match score be 1, mismatch/indel score be -1. What is  $s^*$ ?

 V
 A
 G
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 T
 A
 C
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 C

**Question**: Same scores. What is optimal global alignment and score?

#### Outline

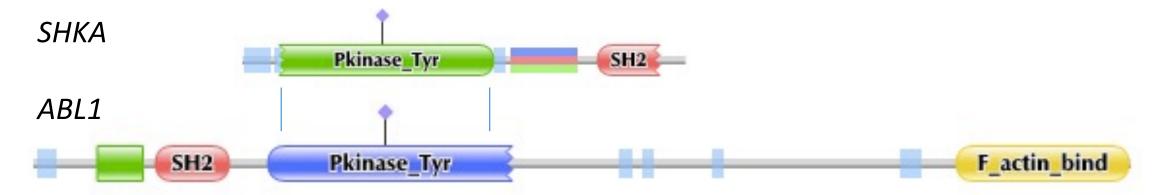
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## Local Alignment – Biological Motivation

Proteins are composed of functional units called domains. Such domains may occur in different proteins even across species.



From Pfam database (<a href="http://pfam.sanger.ac.uk/">http://pfam.sanger.ac.uk/</a>)

**Local Alignment problem:** Given strings  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  and scoring function  $\delta$ , find a substring of  $\mathbf{v}$  and a substring of  $\mathbf{w}$  whose alignment has maximum global alignment score  $s^*$  among *all* global alignments of *all* substrings of  $\mathbf{v}$  and  $\mathbf{w}$ 

## Global, Fitting and Local Alignment

**Global Alignment problem:** Given strings  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  and scoring function  $\delta$ , find alignment of  $\mathbf{v}$  and  $\mathbf{w}$  with maximum score.

**Fitting Alignment problem:** Given strings  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  and scoring function  $\delta$ , find an alignment of  $\mathbf{v}$  and a substring of  $\mathbf{w}$  with maximum global alignment score  $s^*$  among *all* global alignments of  $\mathbf{v}$  and *all* substrings of  $\mathbf{w}$ 

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## Local Alignment – Naive Algorithm

**Local Alignment problem:** Given strings  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  and scoring function  $\delta$ , find a substring of  $\mathbf{v}$  and a substring of  $\mathbf{w}$  whose alignment has maximum global alignment score  $s^*$  among *all* global alignments of *all* substrings of  $\mathbf{v}$  and  $\mathbf{w}$ 

#### **Brute force:**

- 1. Generate all pairs  $(\mathbf{v}', \mathbf{w}')$  of substrings of  $\mathbf{v}$  and  $\mathbf{w}$
- 2. For each pair  $(\mathbf{v}', \mathbf{w}')$ , solve global alignment problem.

**Question**: There are  $\binom{m}{2}\binom{n}{2}$  pairs of substrings. But they have different lengths. What is the running time?

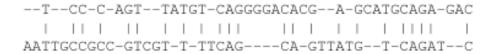
## Key Idea

#### **Global alignment:**

• Start at (0,0) and end at (m,n)

#### **Local alignment**:

Start and end anywhere



tccCAGTTATGTCAGgggacacgagcatgcagagac

aattgccgccgtcgttttcagCAGTTATGTCAGatc

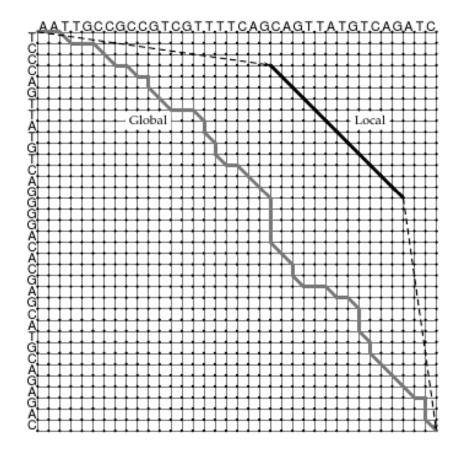


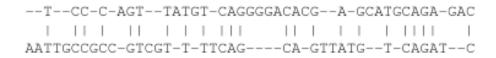
Figure 6.16 (a) Global and (b) local alignments of two hypothetical genes that each have a conserved domain. The local alignment has a much worse score according to the global scoring scheme, but it correctly locates the conserved domain.

## Local Alignment Recurrence

**Local Alignment problem:** Given strings  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  and scoring function  $\delta$ , find a substring of  $\mathbf{v}$  and a substring of  $\mathbf{w}$  whose alignment has maximum global alignment score  $s^*$  among *all* global alignments of *all* substrings of  $\mathbf{v}$  and  $\mathbf{w}$ 

$$s[i,j] = \max \begin{cases} 0, & \text{if } i = 0 \text{ and } j = 0, \\ s[i-1,j] + \delta(v_i, -), & \text{if } i > 0, \\ s[i,j-1] + \delta(-, w_j), & \text{if } j > 0, \\ s[i-1,j-1] + \delta(v_i, w_j), & \text{if } i > 0 \text{ and } j > 0. \end{cases}$$

$$s^* = \max_{i,j} s[i,j]$$



tccCAGTTATGTCAGgggacacgagcatgcagagac

aattgccgccgtcgttttcagCAGTTATGTCAGatc

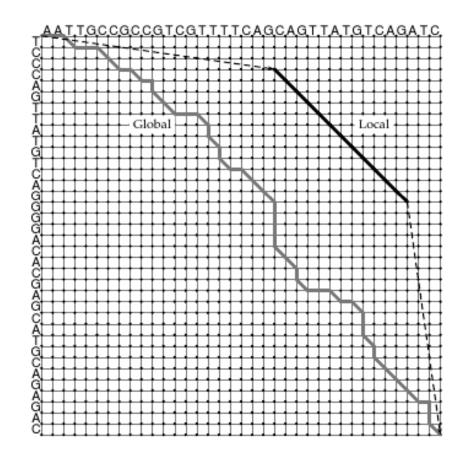


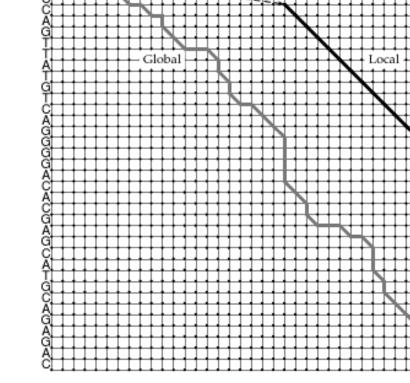
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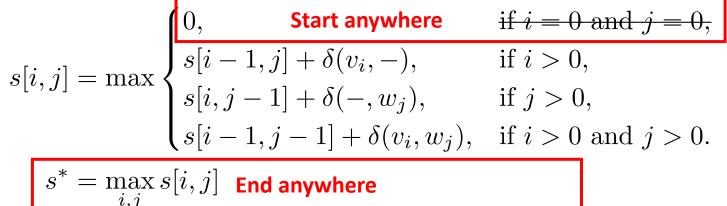


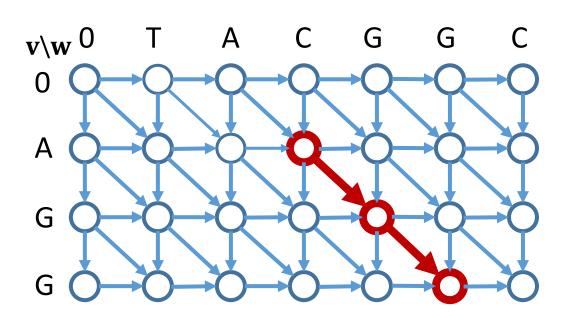


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## Local Alignment – Dynamic Programming

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$$s^* = \max_{i,j} s[i,j]$$

 V
 G
 G

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**Question**: Let match score be 2, mismatch score be -2 and indel be -4. What is  $s^*$ ?

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## Scoring Gaps

Let 
$$\mathbf{v} = AAC$$
 and  $\mathbf{w} = ACAGGC$ 

Match 
$$\delta(c,c)=1$$
;

Mismatch  $\delta(c,d) = -1$  (where  $c \neq d$ ); Indel  $\delta(c,-) = \delta(-,c) = -2$ 

V	A	ı	ı	A	С
W	A	O	A	A	С

V	A	ı	A	_	С
W	A	O	A	A	С

Both alignments have 3 matches and 2 indels.

Score: 
$$(3 * 1) + (2 * -2) = -1$$

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V	A	ı	ı	A	С
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Both alignments have 3 matches and 2 indels.

Score: 
$$(3 * 1) + (2 * -2) = -1$$

Question: Which alignment is better?

## Scoring Gaps – Affine Gap Penalties

**Desired**: Lower penalty for consecutive gaps than interspersed gaps.

**Why**: Consecutive gaps are more likely due to slippage errors in DNA replication (2-3 nucleotides), codons for protein sequences, etc.

V	A	I	I	A	С
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**Affine gap penalty:** Two penalties: (i) gap open penalty  $\rho \geq 0$  and (ii) gap extension penalty  $\sigma \geq 0$ . Stretch of k consecutive gaps has score  $-(\rho + \sigma k)$ .

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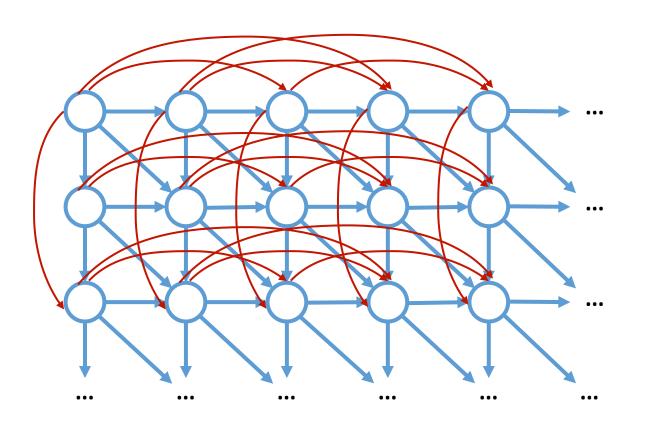
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Let 
$$\rho = 10$$
 and  $\sigma = 1$ . Left:  $(3*1) - (10+1*2) = -9$ . Right:  $(3*1) - (10+1*1) - (10+1*1) = -19$ .

## Affine Gap Penalty Alignment – Naive Approach

Affine gap penalty: Two penalties: (i) gap open penalty  $\rho \ge 0$  and (ii) gap extension penalty  $\sigma \ge 0$ . Stretch of k consecutive gaps has score  $-(\rho + \sigma k)$ .



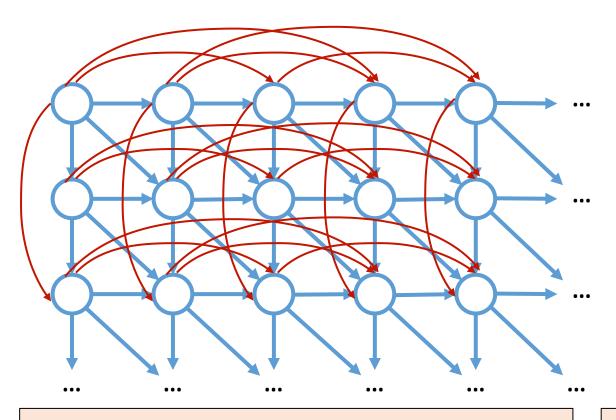
Idea: Insert horizontal (deletion) and vertical (insertion) edges spanning k > 1 gaps with score  $-(\rho + \sigma k)$ .

new edges

old edges

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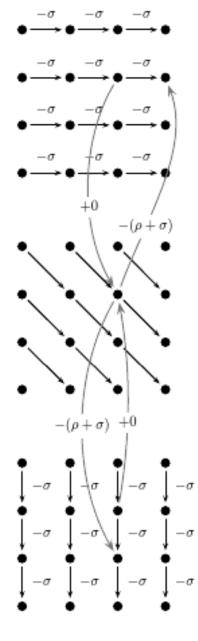
Question: What's the recurrence?

**Question**: What's the running time?

# Affine Gap Penalty Alignment

**Idea**: Three separate recurrences:

- (i) Gap in first sequence  $s^{\rightarrow}[i,j]$ 
  - (ii) Match/mismatch  $s^{\searrow}[i,j]$
- (iii) Gap in second sequence  $s^{\downarrow}[i,j]$



**Figure 6.18** A three-level edit graph for alignment with affine gap penalties. Every vertex (i,j) in the middle level has one outgoing edge to the upper level, one outgoing edge to the lower level, and one incoming edge each from the upper and lower levels.

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$$\begin{split} s^{\to}[i,j] &= \max \begin{cases} s^{\to}[i,j-1] - \sigma, & \text{if } j > 1, \\ s^{\searrow}[i,j-1] - (\sigma + \rho), & \text{if } j > 0, \end{cases} \\ s^{\searrow}[i,j] &= \max \begin{cases} 0, & \text{if } i = 0 \text{ and } j = 0, \\ s^{\to}[i,j], & \text{if } j > 0, \\ s^{\searrow}[i,j], & \text{if } i > 0, \\ s^{\searrow}[i-1,j-1] + \delta(v_i,w_j), & \text{if } i > 0 \text{ and } j > 0, \end{cases} \\ s^{\downarrow}[i,j] &= \max \begin{cases} s^{\downarrow}[i-1,j] - \sigma, & \text{if } i > 1, \\ s^{\searrow}[i-1,j] - (\sigma + \rho), & \text{if } i > 0. \end{cases} \end{split}$$

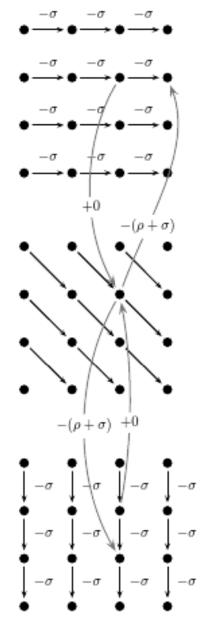


Figure 6.18 A three-level edit graph for alignment with affine gap penalties. Every vertex (i, j) in the middle level has one outgoing edge to the upper level, one outgoing edge to the lower level, and one incoming edge each from the upper and lower levels.

# Affine Gap Penalty Alignment

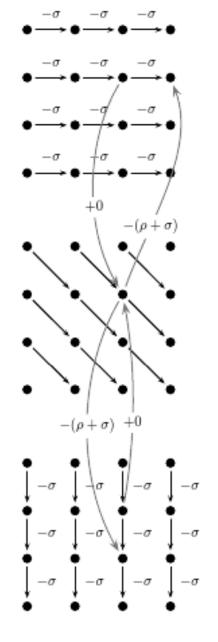
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$$s^{\rightarrow}[i,j] = \max \begin{cases} s^{\rightarrow}[i,j-1] - \sigma, & \text{if } j > 1, \\ s^{\searrow}[i,j-1] - (\sigma + \rho), & \text{if } j > 0, \end{cases}$$

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$$s^{\downarrow}[i,j] = \max \begin{cases} s^{\downarrow}[i-1,j] - \sigma, & \text{if } i > 1, \\ s^{\searrow}[i-1,j] - (\sigma + \rho), & \text{if } i > 0. \end{cases}$$



Running time: O(mn)

**Figure 6.18** A three-level edit graph for alignment with affine gap penalties. Every vertex (i,j) in the middle level has one outgoing edge to the upper level, one outgoing edge to the lower level, and one incoming edge each from the upper and lower levels.

## Affine Gap Penalty Alignment – Example

Let  $\rho=10$  and  $\sigma=1$ . Match = 1. Mismatch = -1

$$\mathbf{v} = AAC$$

#### $\mathbf{w} = ACAAC$

$$s^{\rightarrow}[i,j] = \max \begin{cases} s^{\rightarrow}[i,j-1] - \sigma, & \text{if } j > 1, \\ s^{\searrow}[i,j-1] - (\sigma + \rho), & \text{if } j > 0, \end{cases}$$

$$s^{\searrow}[i,j] = \max \begin{cases} 0, & \text{if } i = 0 \text{ and } j = 0, \\ s^{\Rightarrow}[i,j], & \text{if } j > 0, \\ s^{\downarrow}[i,j], & \text{if } i > 0, \\ s^{\searrow}[i-1,j-1] + \delta(v_i,w_j), & \text{if } i > 0 \text{ and } j > 0, \end{cases}$$

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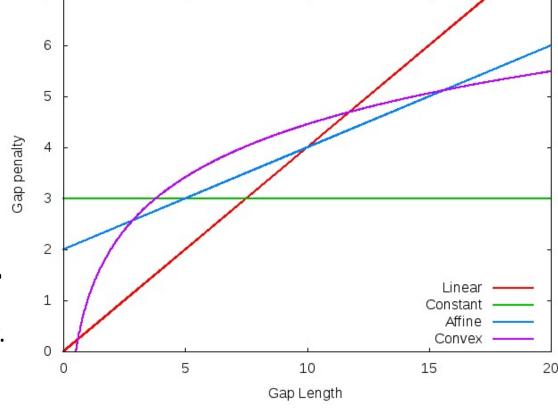
See recording!

## Gapped Alignment – Additional Insights

• Naive approach supports arbitrary gap penalties given two sequences  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$ . This results in an O(mn(m+n)) algorithm.

• Alignment with **convex gap penalties** given two sequences  $\mathbf{v} \in \Sigma^m$  and  $\mathbf{w} \in \Sigma^n$  can be computed in  $O(mn \log m)$  time.

See: Dan Gusfield. 1997. Algorithms on Strings, Trees, and Sequences: Computer Science and Computational Biology. Cambridge University Press, New York, NY, USA.



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### Substitution Matrices

- Given a pair (v, w) of aligned sequences, we want to assign a score that
  measure the relative likelihood that the sequences are related as opposed
  to being unrelated
- We need two models:
  - Random model R: each letter  $a \in \Sigma$  occurs independently with probability  $q_a$
  - Match model M: aligned pair  $(a,b) \in \Sigma \times \Sigma$  occur with joint probability  $p_{a,b}$

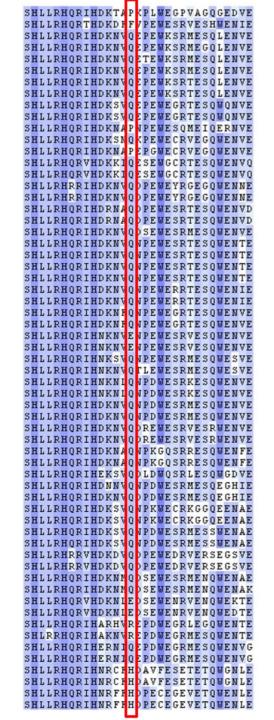
$$\Pr(\mathbf{v}, \mathbf{w} | R) = \prod_{i} q_{v_i} \cdot \prod_{i} q_{w_i}$$

$$\Pr(\mathbf{v}, \mathbf{w} | M) = \prod_{i} p_{v_i, w_i}$$

$$\log \frac{\Pr(\mathbf{v}, \mathbf{w} | M)}{\Pr(\mathbf{v}, \mathbf{w} | R)} = \sum_{i} s(v_i, w_i) \text{ where } s(a, b) = \ln \frac{p_{a,b}}{q_a q_b}$$

## BLOSUM (<u>Blo</u>cks <u>Su</u>bstitution <u>M</u>atrices)

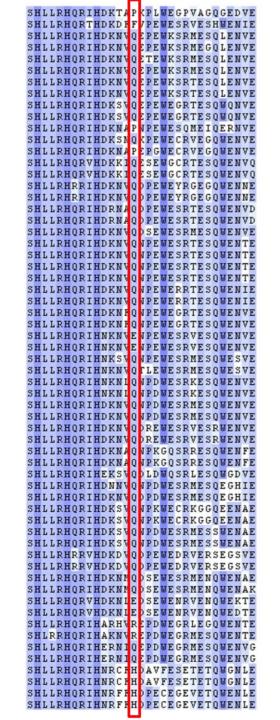
- Henikoff and Henikoff, 1992
- Computed using **ungapped** alignments of protein segments (blocks) from BLOCKS database
- Thousands of such blocks go into computing a single BLOSUM matrix
- Example of a one such block (right):
  - 31 positions (columns)
  - 61 sequences (rows)
- Given threshold *L*, block is pruned down to largest set *C* of sequences that have at least *L*% sequence identity to another sequence in *C* 
  - How to compute C?



# BLOSUM (Blocks Substitution Matrices)

$$\log \frac{\Pr(\mathbf{v}, \mathbf{w}|M)}{\Pr(\mathbf{v}, \mathbf{w}|R)} = \sum_{i} s(v_i, w_i) \text{ where } s(a, b) = \frac{1}{\lambda} \ln \frac{p_{a,b}}{q_a q_b}$$

- Null model frequencies  $q_a q_b$  of letters a and b:
  - Count the number of occurrences of a (b) in all blocks
  - Divide by sum of lengths of each block (sequences \* positions)
- Match model frequency  $p_{a,b}$ :
  - Count the number of pairs (a, b) in all columns of all blocks
  - Divide by the total number of pairs of columns:
    - $\sum_{C} n(C) {m(C) \choose 2}$
    - m(C) is the number of sequences in block C
    - n(C) is the number of positions in block C



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#### Example: $(\lambda = 0.5)$

$$q_{A} = \frac{7}{15}$$
A A T
 $q_{T} = \frac{3}{15}$ 
S A L
 $p_{A,T} = \frac{4}{30}$ 
T A V
A A L
 $s(A,T) = 2 \cdot \ln \frac{4}{7} \cdot \frac{3}{15} \approx 0.7$ 

## BLOSUM62

$$\log \frac{\Pr(\mathbf{v}, \mathbf{w} | M)}{\Pr(\mathbf{v}, \mathbf{w} | R)} = \sum_{i} s(v_i, w_i) \text{ where } s(a, b) = \frac{1}{\lambda} \ln \frac{p_{a,b}}{q_a q_b}$$

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Arg
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                   6
Asn
                         6
Asp
Cys
                                     5
Gln
                         0
      -1
Glu
Gly
        0
                                               6
His
lle
                                                               4
Leu
Lys
Met
                                     0
```

This explains some details in BLOSUM62 that may seem counterintuitive at first glance. For instance, tryptophan (W/W) pairs score +11, while leucine (L/L) pairs only score +4; why shouldn't all identitites get the same score? The rarer the amino acid is, the more surprising it would be to see two of them align together by chance. In the homologous alignment data that BLOSUM62 was trained on, leucine/leucine (L/L) pairs were in fact more common than tryptophan/tryptophan (W/W) pairs ( $p_{\rm LL}=0.0371,\,p_{\rm WW}=0.0065$ ), but tryptophan is a much rarer amino acid ( $f_{\rm L}=0.099,\,f_{\rm W}=0.013$ ). Run those numbers (with BLOSUM62's original  $\lambda=0.347$ ) and you get +3.8 for L/L and +10.5 for W/W, which were rounded to +4 and +11.

https://doi.org/10.1038/nbt0804-1035

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## Take Home Messages

- 1. Edit distance
- 2. Global alignment
- 3. Fitting alignment
- 4. Local alignment
- 5. Gapped alignment
- 6. BLOSUM substitution matrix

Edit distance is shortest path in DAG

Global alignment is longest path in DAG

Small tweaks enable different extensions

#### Reading:

- Jones and Pevzner. Chapters 6.6-6.9
- Lecture notes